

# High energy pA collisions in CGC

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OF SCIENCE AND TECHNOLOGY

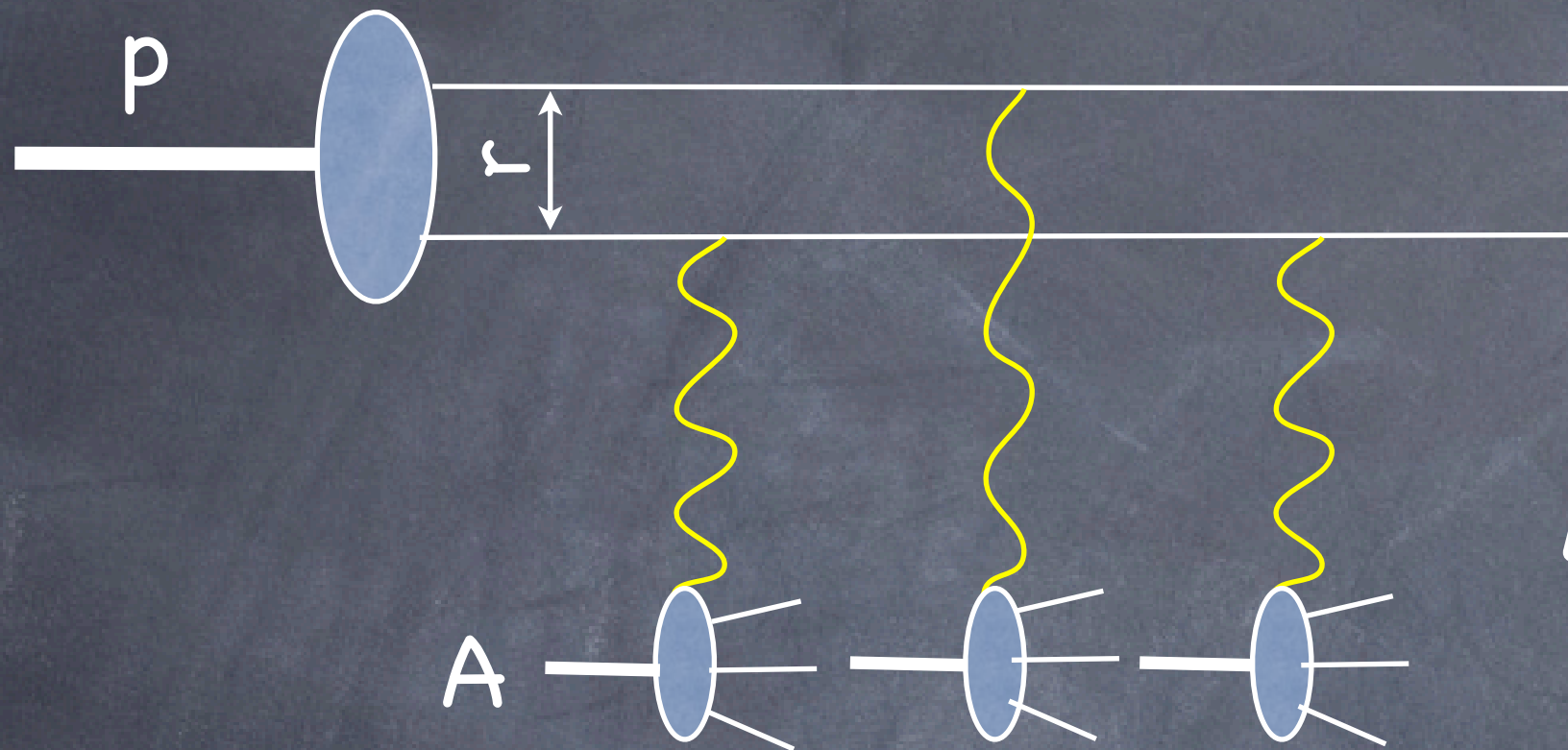
*RIKEN BNL Research Center*

Nuclei as heavy as bulls through collision generate new states of matter



Hard Probes 2006, CA

# Quasiclassical picture of pA collisions



• Kinematic regime:  $x \ll 1$ ,  $\alpha \ll 1$

• Coherence length of qq pair

$$l_c \approx \frac{1}{k_-^q + k_-^{\bar{q}} - k_-^h} = \frac{1}{M_N x} \gg R_A$$

with  $x = \frac{m_\perp}{\sqrt{s}} e^{-y}$

The dipole-nucleus cross section  $\sigma_{q\bar{q}} = 2 \int d^2 \underline{b} \text{Im} N(x, \underline{r}, \underline{b})$

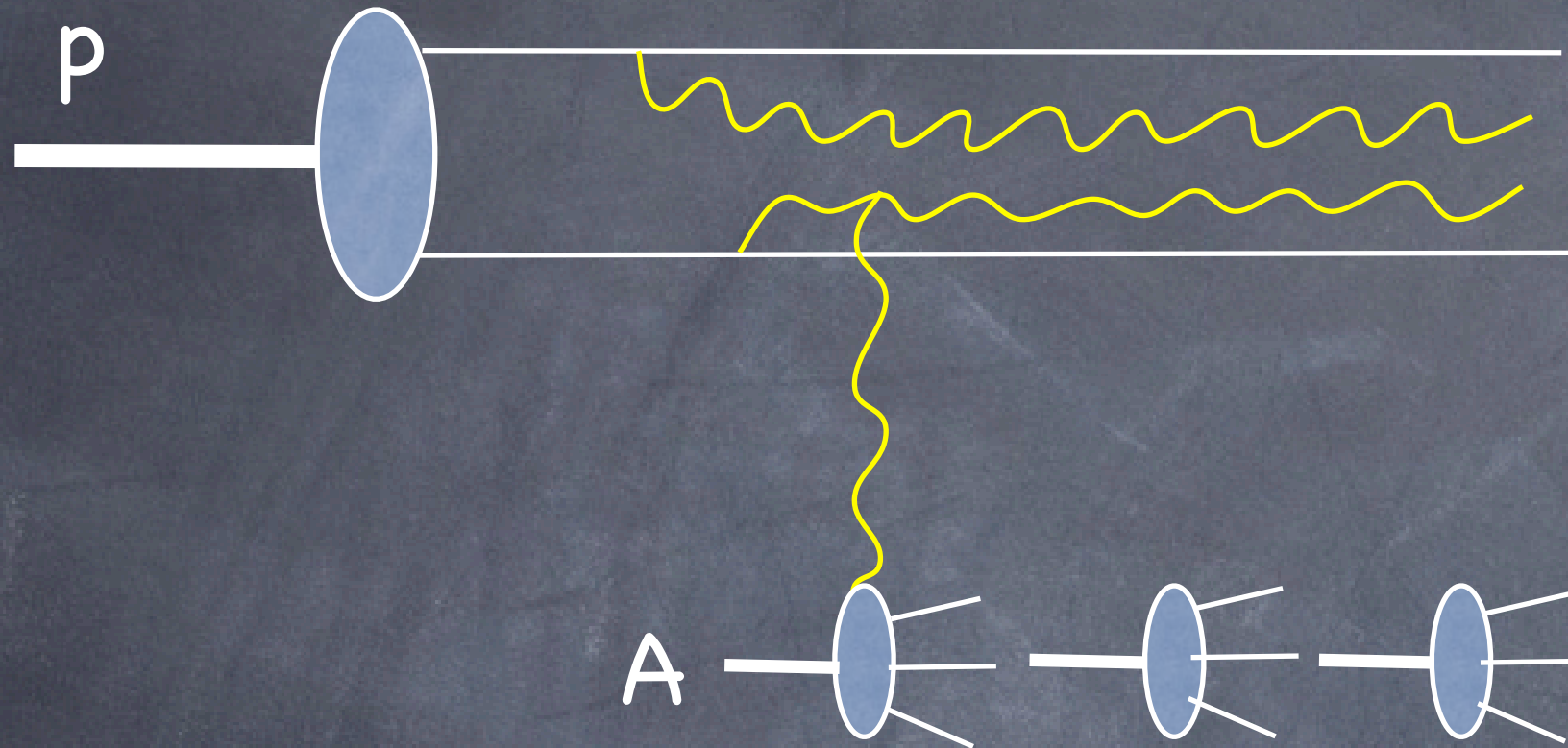
Quasiclassical-approximation:  $\alpha_s \ln(1/x) \ll 1$      $\alpha_s^2 A^{1/3} \sim 1$

$$\text{Im} N(x, \underline{r}, \underline{b}) = 1 - \exp \left( -\underline{r}^2 Q_s^2 / 4 \right)$$

A. Mueller,  
McLerran-Venugopalan



# Linear evolution

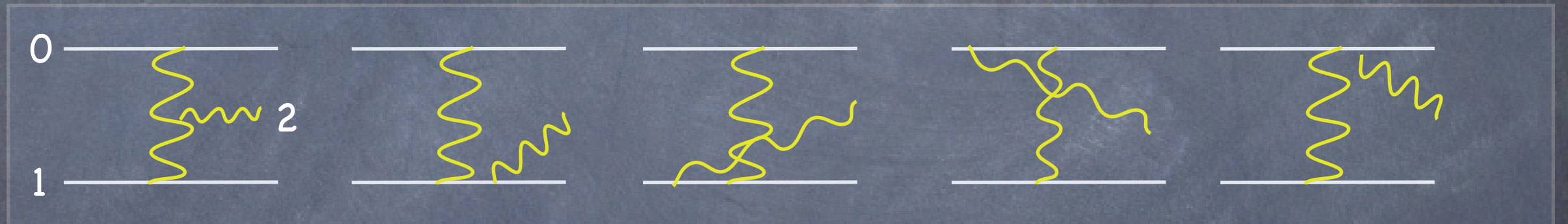
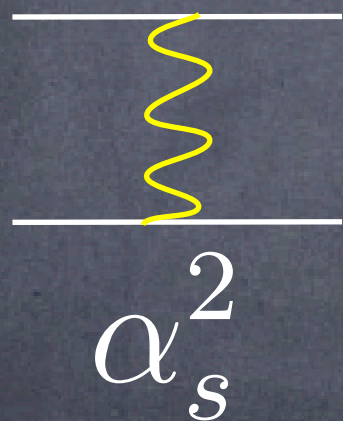


• Linear evolution regime

$$\alpha_s \ln(1/x) \sim 1 \quad \alpha_s^2 A^{1/3} \ll 1$$

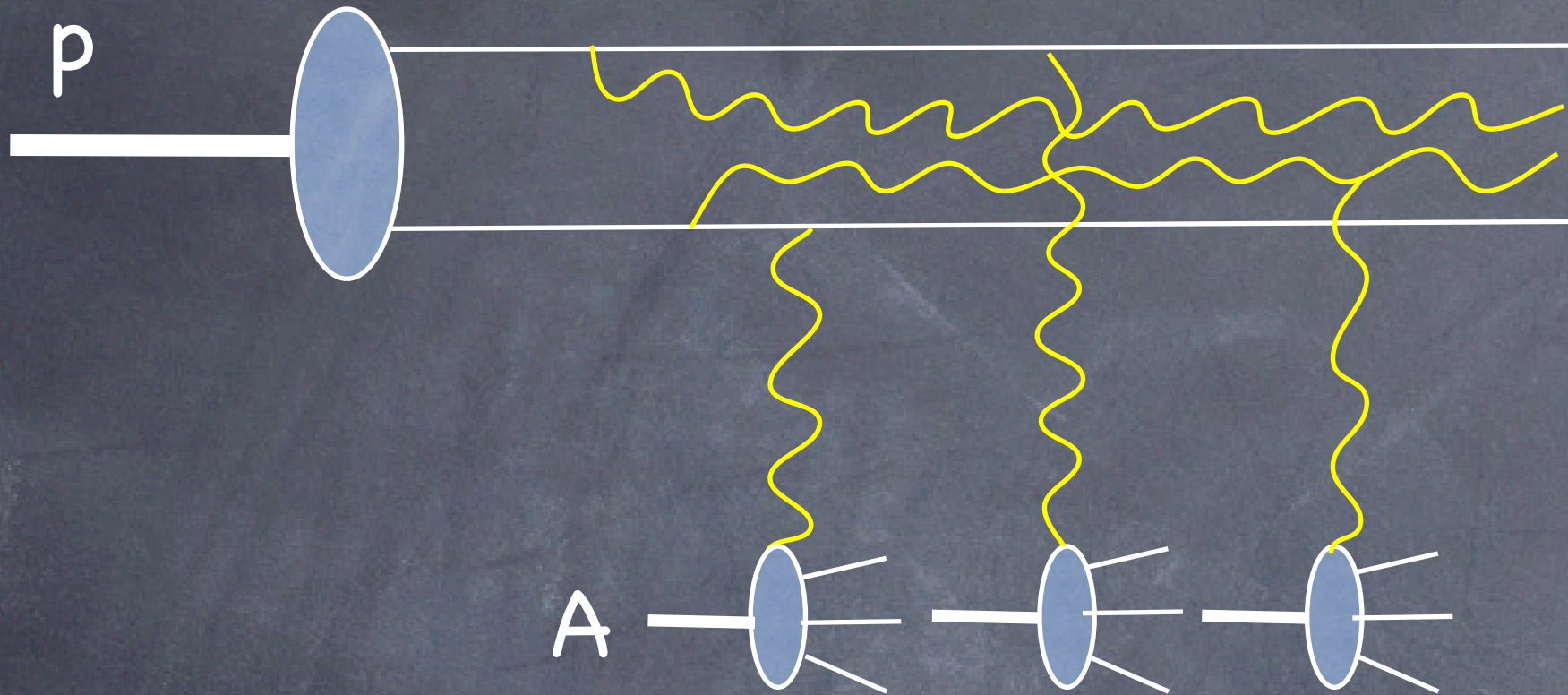
(BFKL)

COM:



$$\partial_y N(\underline{x}_{01}) = \frac{\alpha_s}{2\pi} \int d^2 x_2 \frac{\underline{x}_{01}^2}{\underline{x}_{12}^2 \underline{x}_{20}^2} (N(\underline{x}_{12}) + N(\underline{x}_{20}) - N(\underline{x}_{01}))$$

# High parton density



- Non-linear evolution regime

$$\alpha_s \ln(1/x) \sim 1, \quad \alpha_s^2 A^{1/3} \sim 1$$

$$\partial_y N(\underline{x}_{01}) = \frac{\alpha_s}{2\pi} \int d^2 x_2 \frac{\underline{x}_{01}^2}{\underline{x}_{12}^2 \underline{x}_{20}^2} (N(\underline{x}_{12}) + N(\underline{x}_{20}) - N(\underline{x}_{01}) - N(\underline{x}_{12})N(\underline{x}_{20}))$$

Balitski, Kovchegov

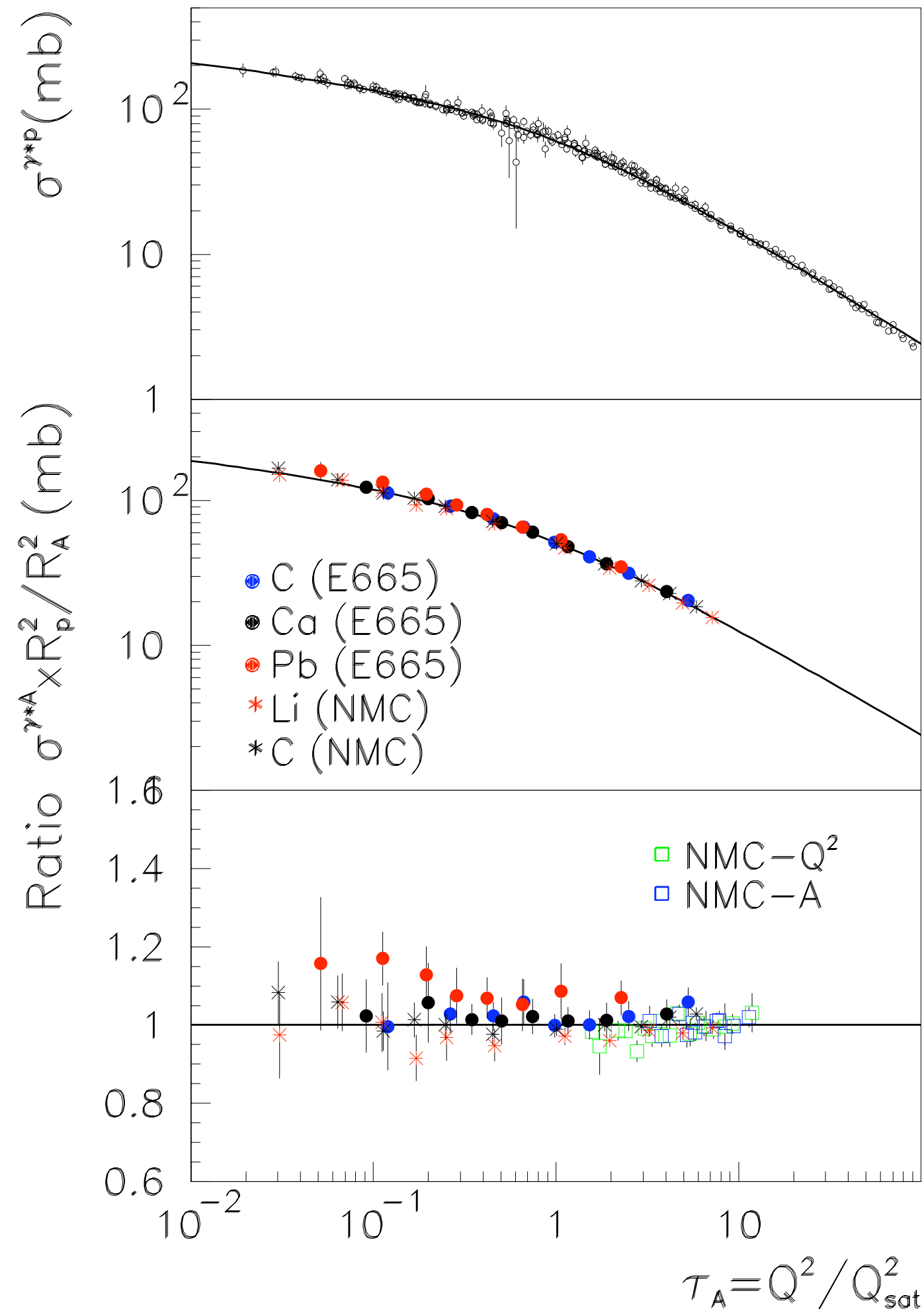
The saturation scale  $Q_s^2 = \Lambda^2 A^{1/3} e^{\lambda y} e^{\lambda s/2}$

- Effective theory of high parton density QCD is "Color Glass Condensate".

JIMWLK



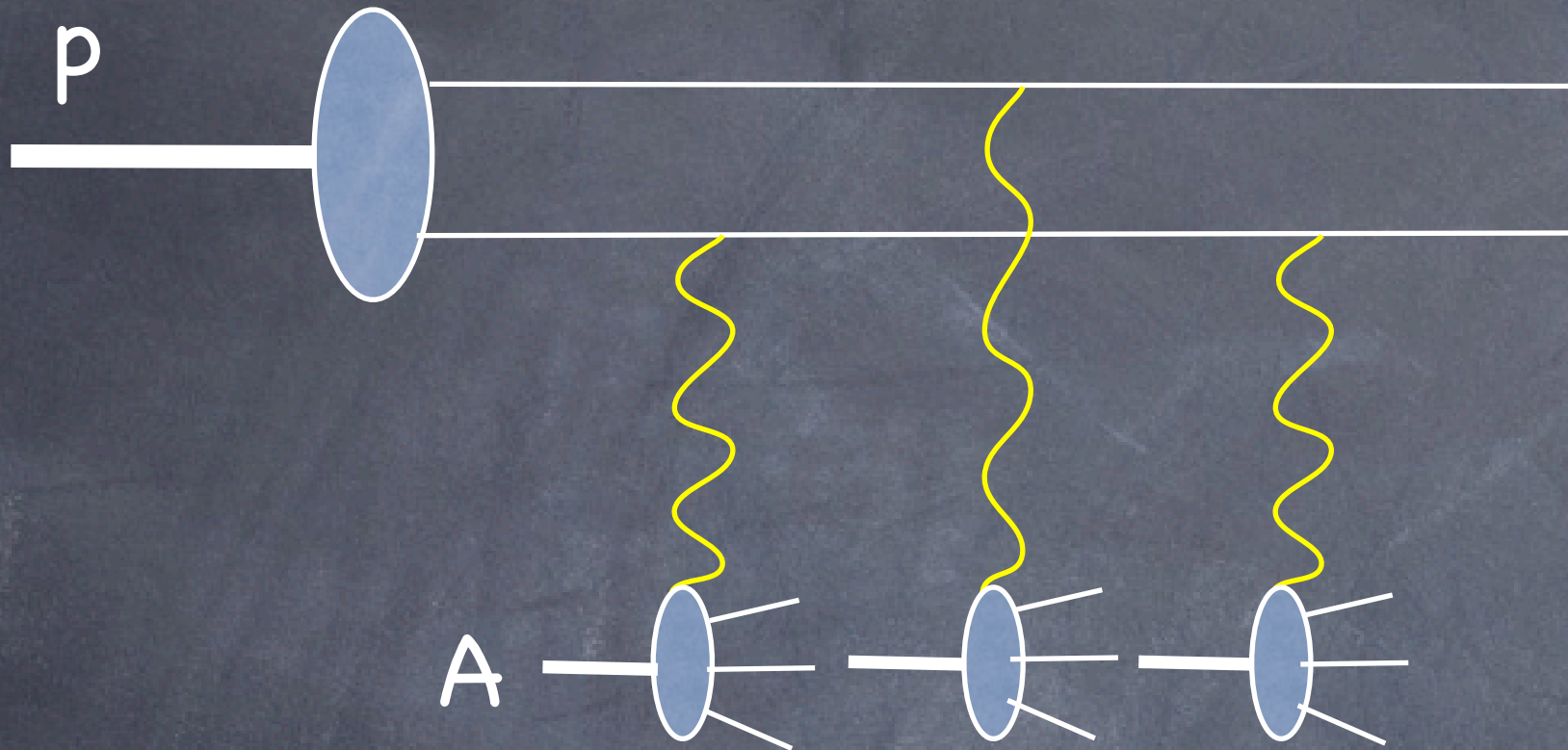
# Geometric scaling in nuclei



- Scaling of DIS cross section with  $Q/Q_s$  is the direct signal of high parton density.

Stasto, Golec-Biernat, Kwiecinski  
Armesto, Salgado, Wiedemann

# Gluon Production



- Gluon interaction with the nucleus is instantaneous:

$$l_c = \frac{k_+}{k_\perp^2} \gg R_A$$

Kovchegov, A. Mueller; Kovchegov, KT

$$\frac{d\sigma^{pA}}{d^2k dy} = \frac{2\alpha_s}{C_F k_\perp^2} \int d^2q \phi_p(\underline{q}, Y - y) \phi_A(\underline{k} - \underline{q}, y)$$

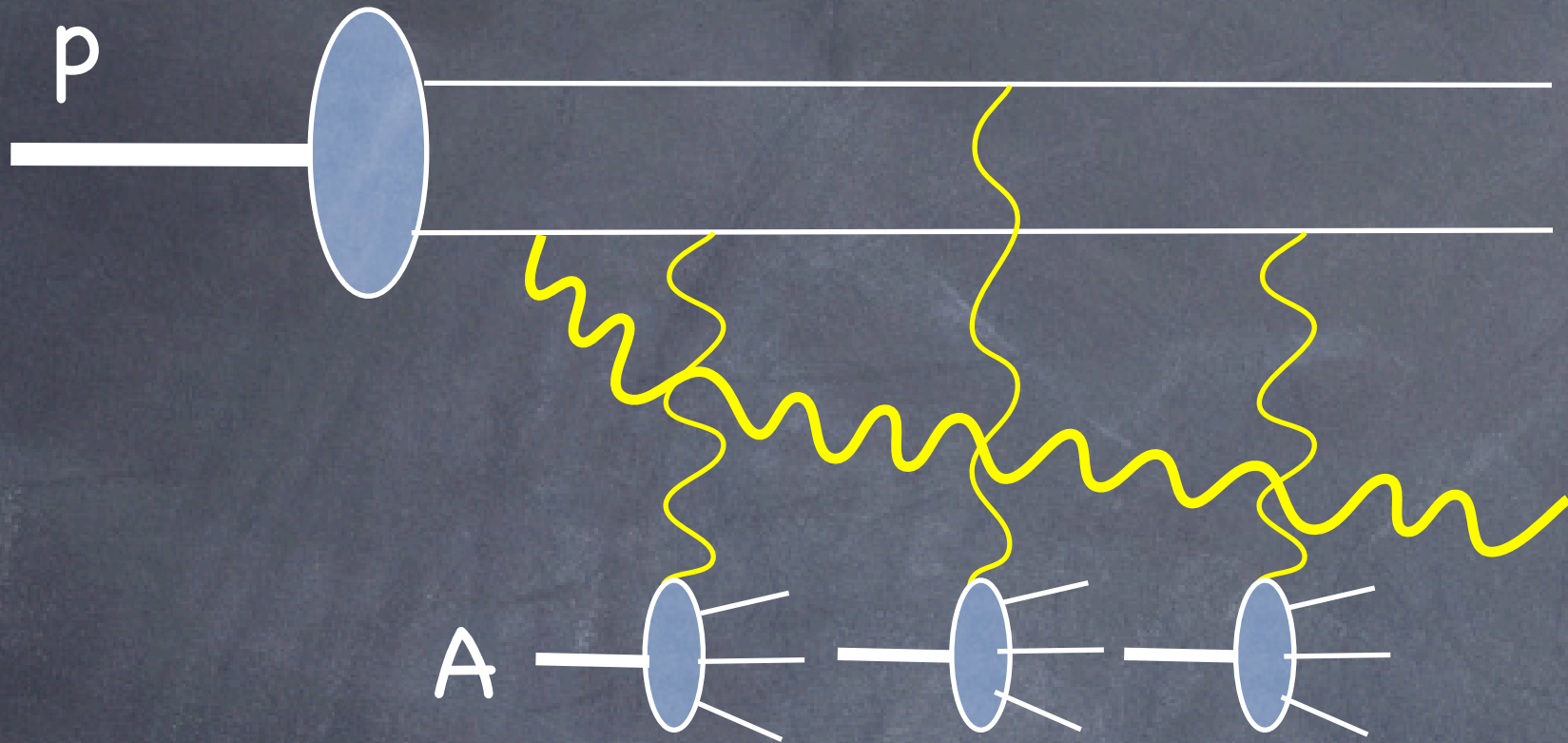
**where**  $\phi(x, \underline{k}^2) = \frac{C_F}{\alpha_s (2\pi)^3} \int d^2b d^2z e^{-i\underline{k} \cdot \underline{z}} \nabla_z^2 N_G(\underline{z}, \underline{b}, y)$

is unintegrated gluon distribution function

see also Dumitru, McLerran



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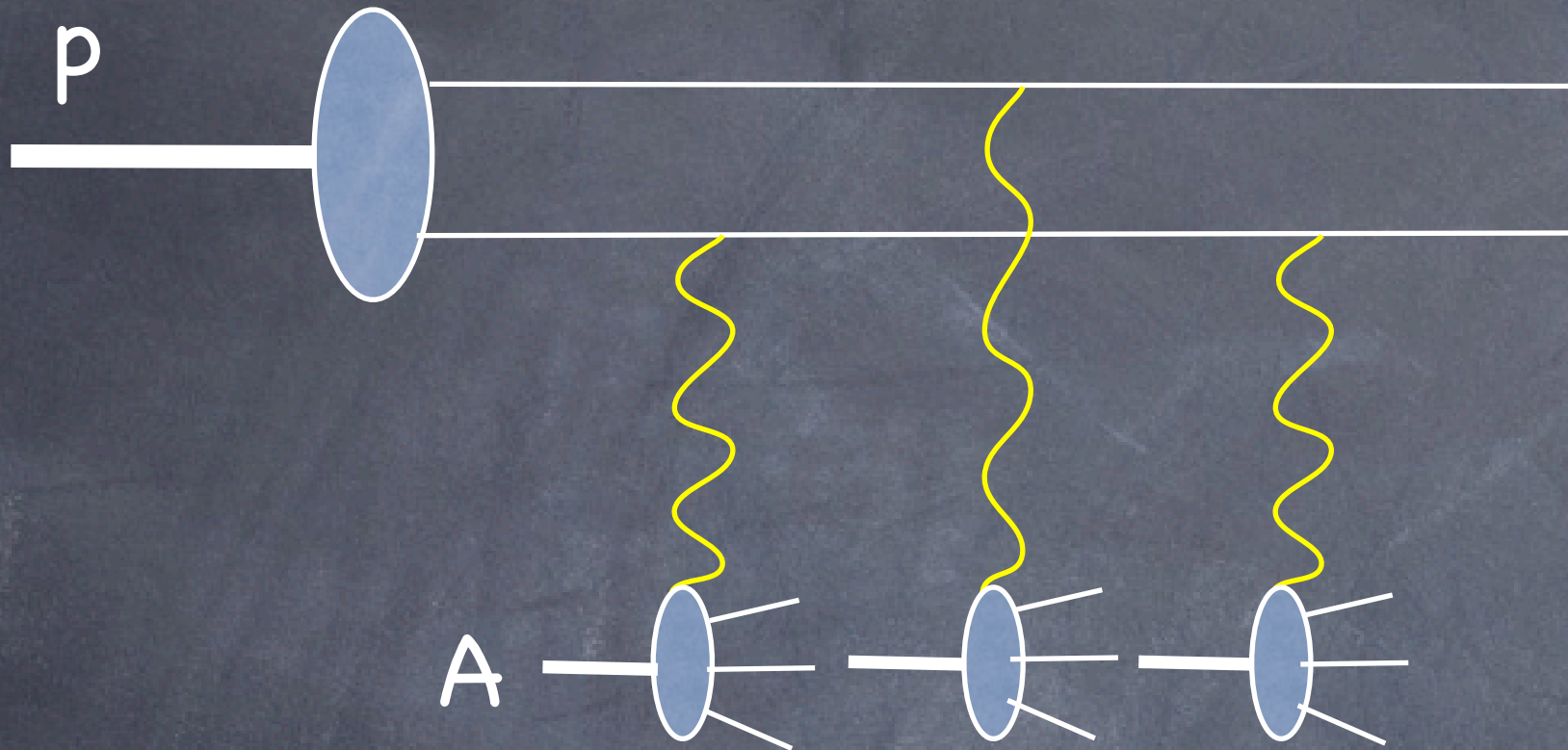
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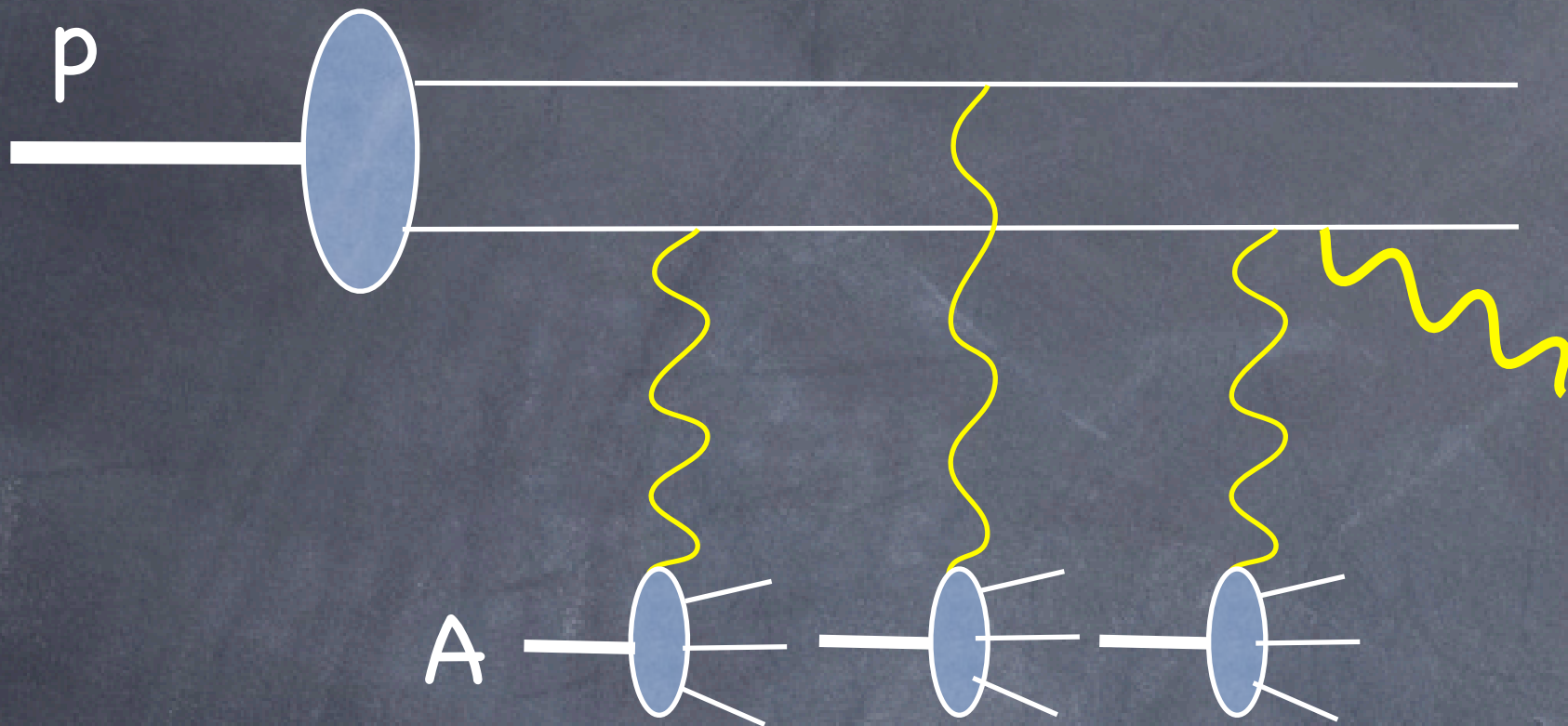
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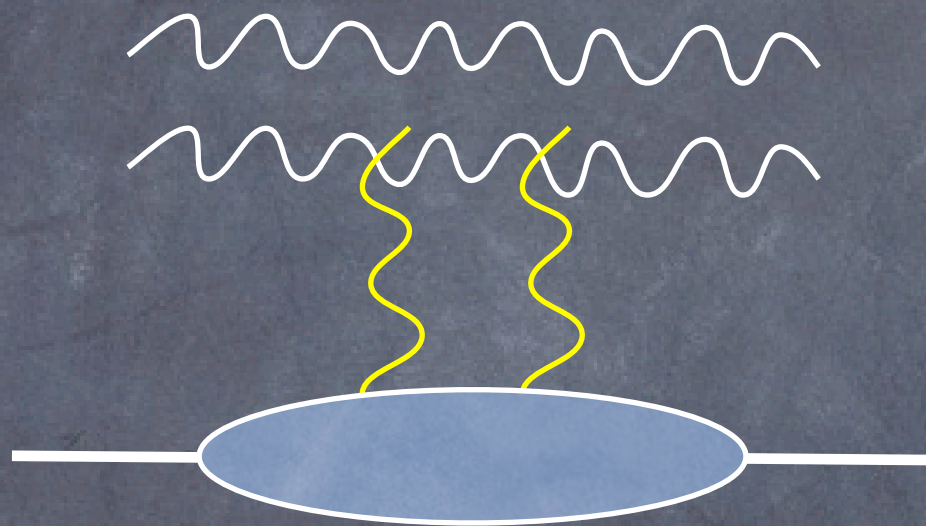
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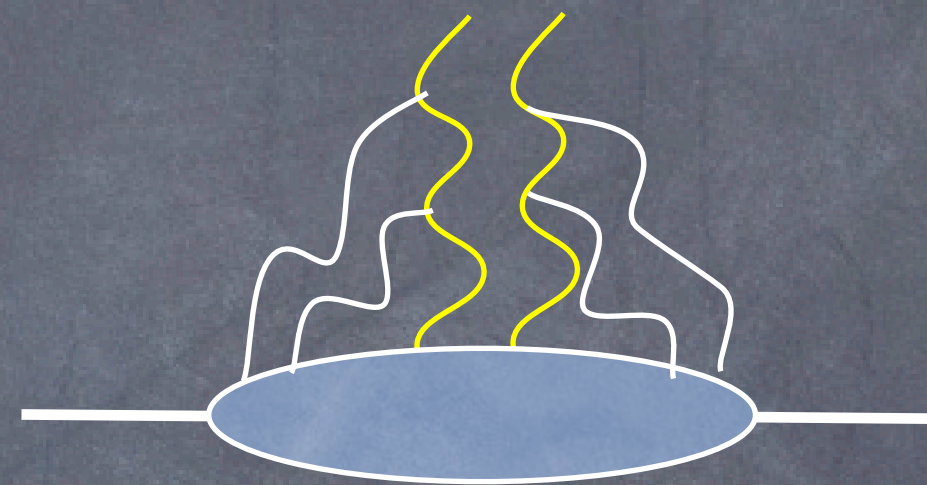
see also Dumitru, McLerran

# $k_T$ -factorization (Levin, Ryskin)

- In spite of explicit factorization breaking by each individual diagram, their sum can be factorized. (Kovchegov, KT) AGK rules?



Factorized gluon  
distribution



Weizsäcker-Williams  
gluon distribution

- No gauge is known in which the factorization would be explicit.



# CGC vs shadowing models

- it's all about parameters

$x$



How small is  $x$ ? Is  $l_c \gg R_A$ ?

$\alpha_s^2 A^{1/3}$



Is  $A$  large enough to make higher twist effects important?

$\alpha_s \ln(1/x)$

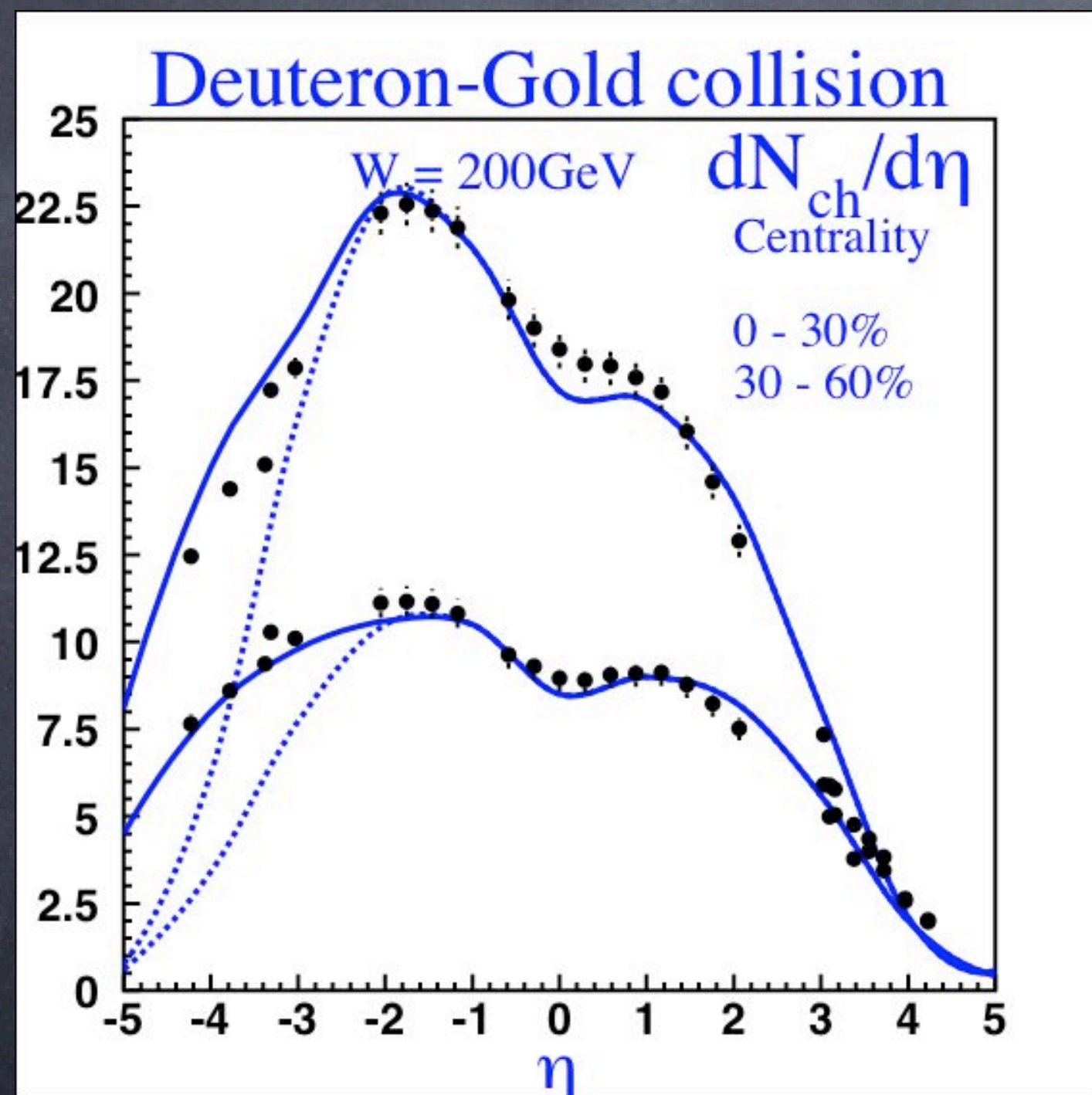


Is  $x$  small enough to generate quantum evolution?

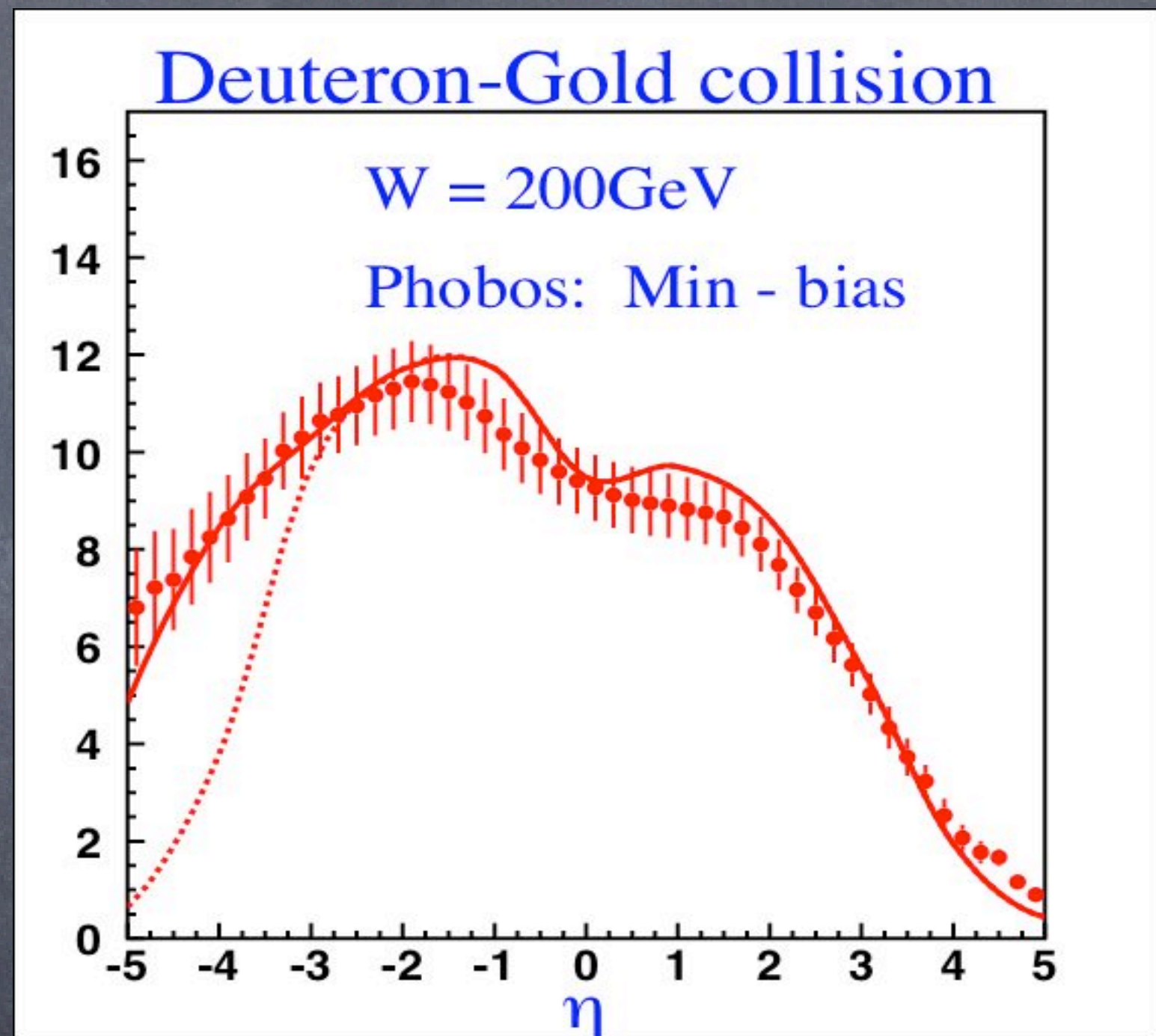
- CGC resums higher twists and evolution logarithms at  $x \ll 1$ . Requires modeling to match onto  $x \sim 1$ ,  $Q \rightarrow \infty$  physics.
- Shadowing models take into account only one high parton density effect at a time but match well onto  $x \sim 1$ ,  $Q \rightarrow \infty$ .

# Hadron multiplicities in dAu at RHIC

- Total multiplicities (Kharzeev, Levin, Nardi)



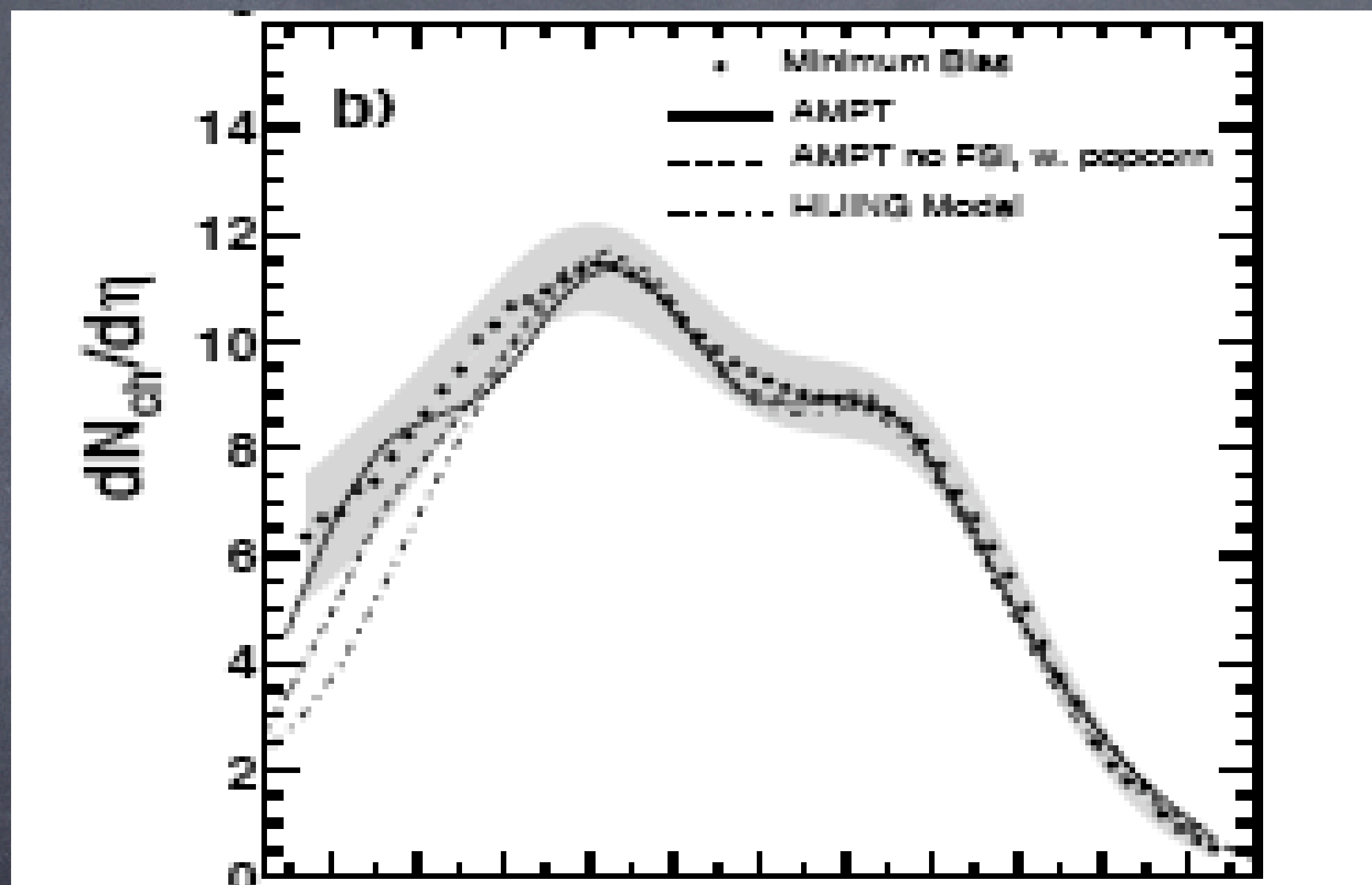
BRAHMS



PHOBOS



# Multiplicity by other models



by PHOBOS

# Pseudo-rapidity asymmetry

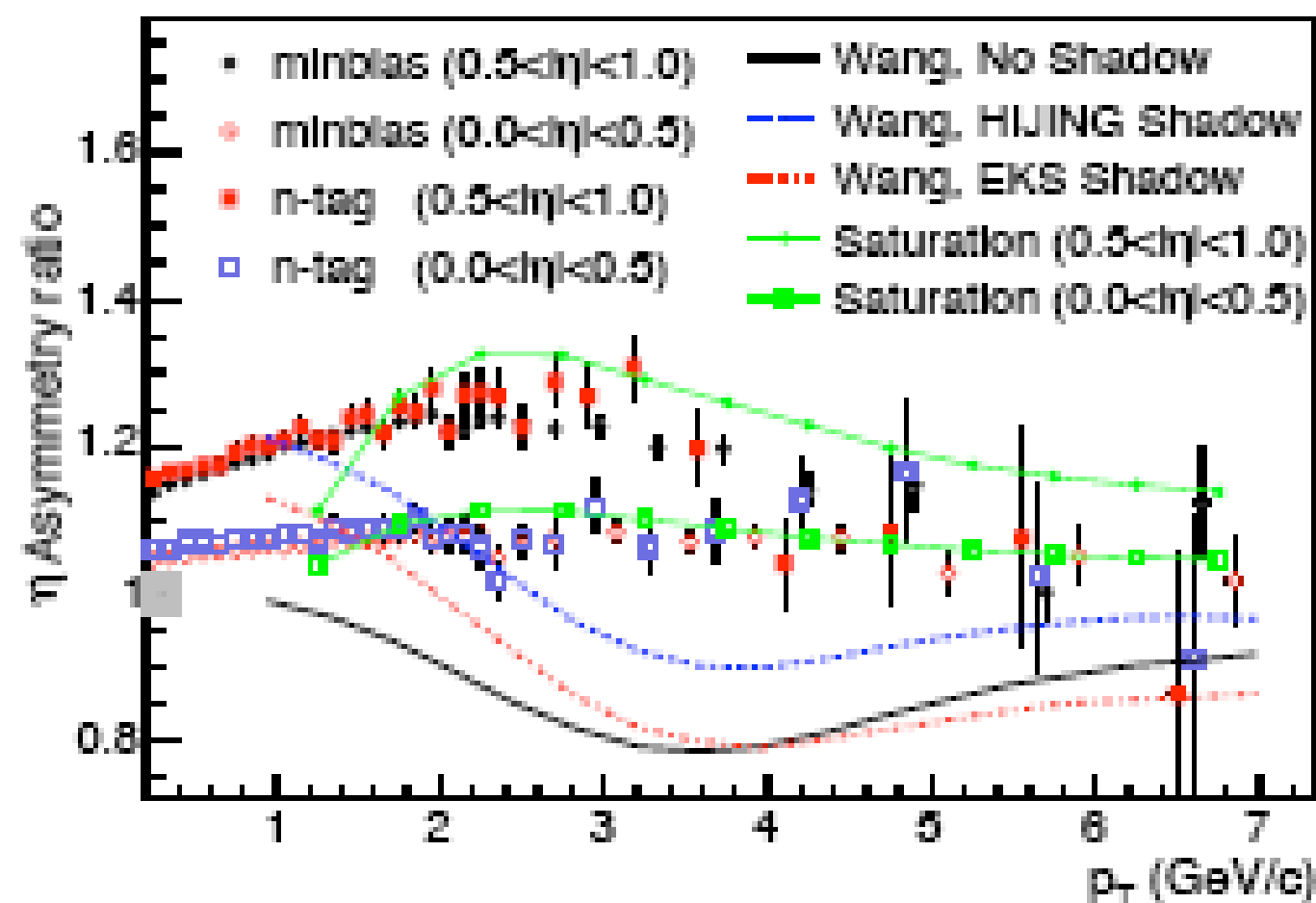


FIG. 3: (Color online) The ratio of charged hadron spectra in the backward rapidity to forward rapidity region for minimum bias and ZDC-d neutron-tagged events. Calculations based on pQCD [3] ( $y = -1/y = 1$ ) for minimum bias events are also shown for cases with no shadowing (solid curve), HIJING shadowing (dashed curve), and EKS shadowing (dot-dashed curve). Calculations in a gluon saturation model [13] for minimum bias events are shown for  $0.5 < |\eta| < 1.0$  (filled circles with solid line) and for  $0.0 < |\eta| < 0.5$  (open squares with solid line).

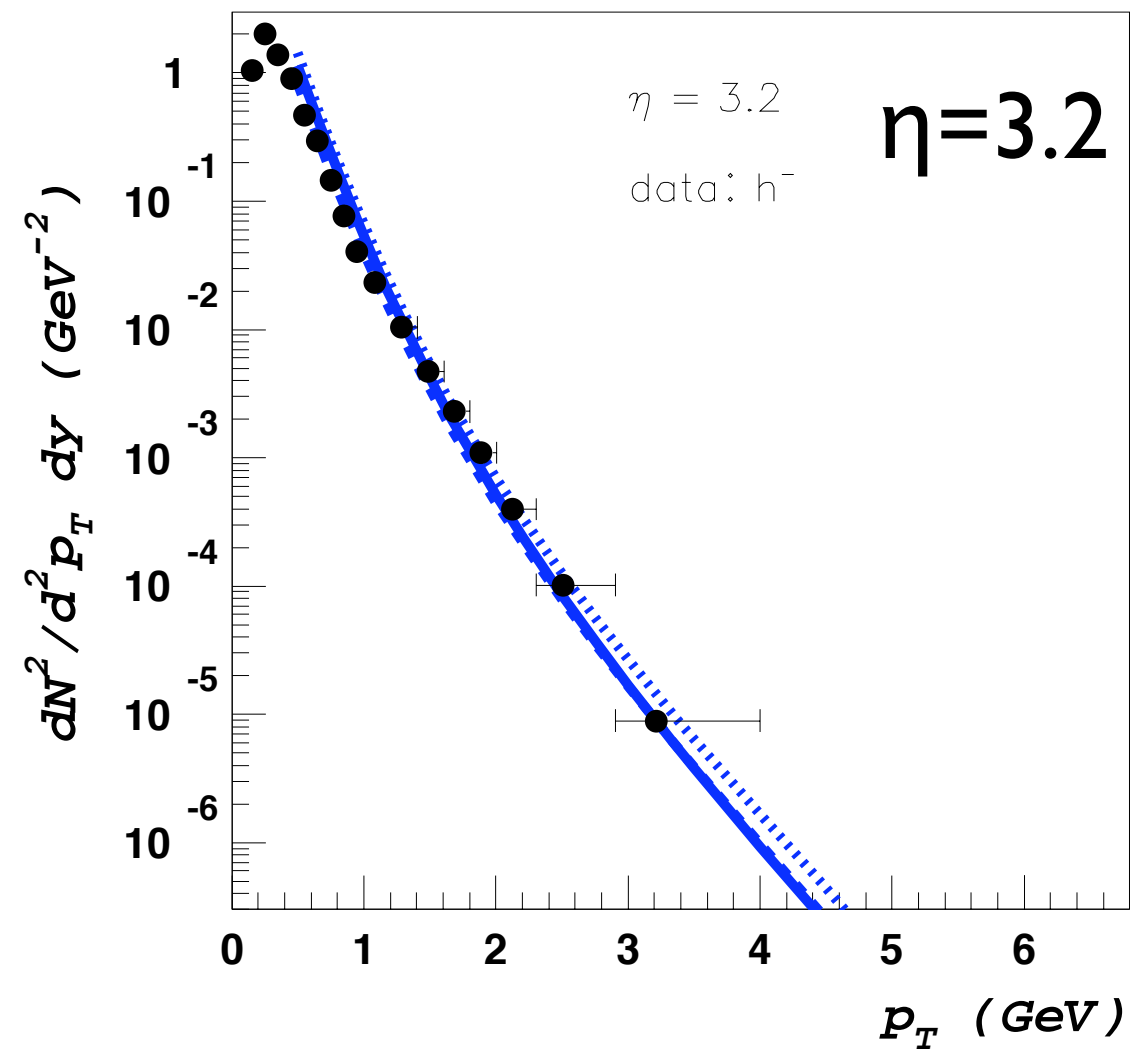
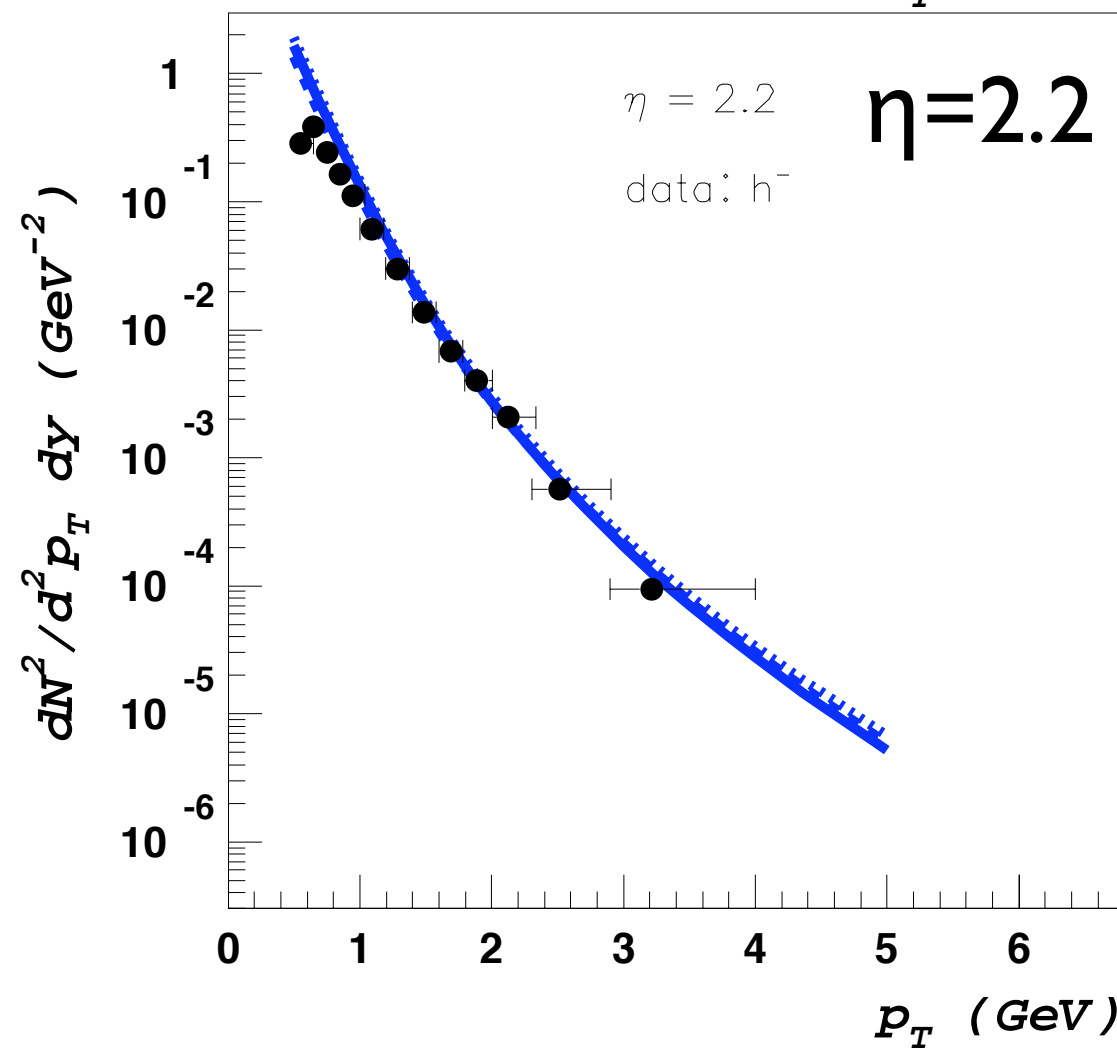
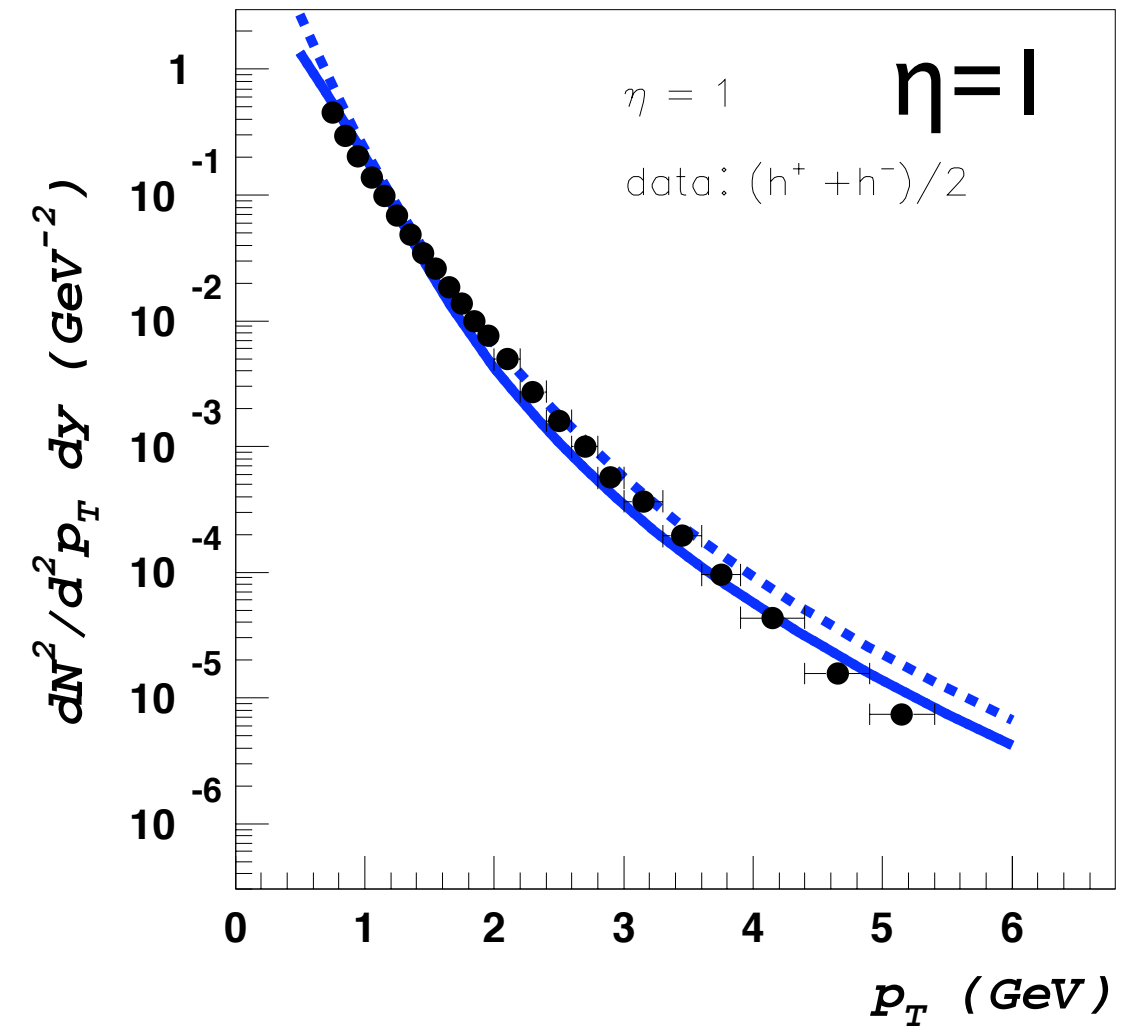
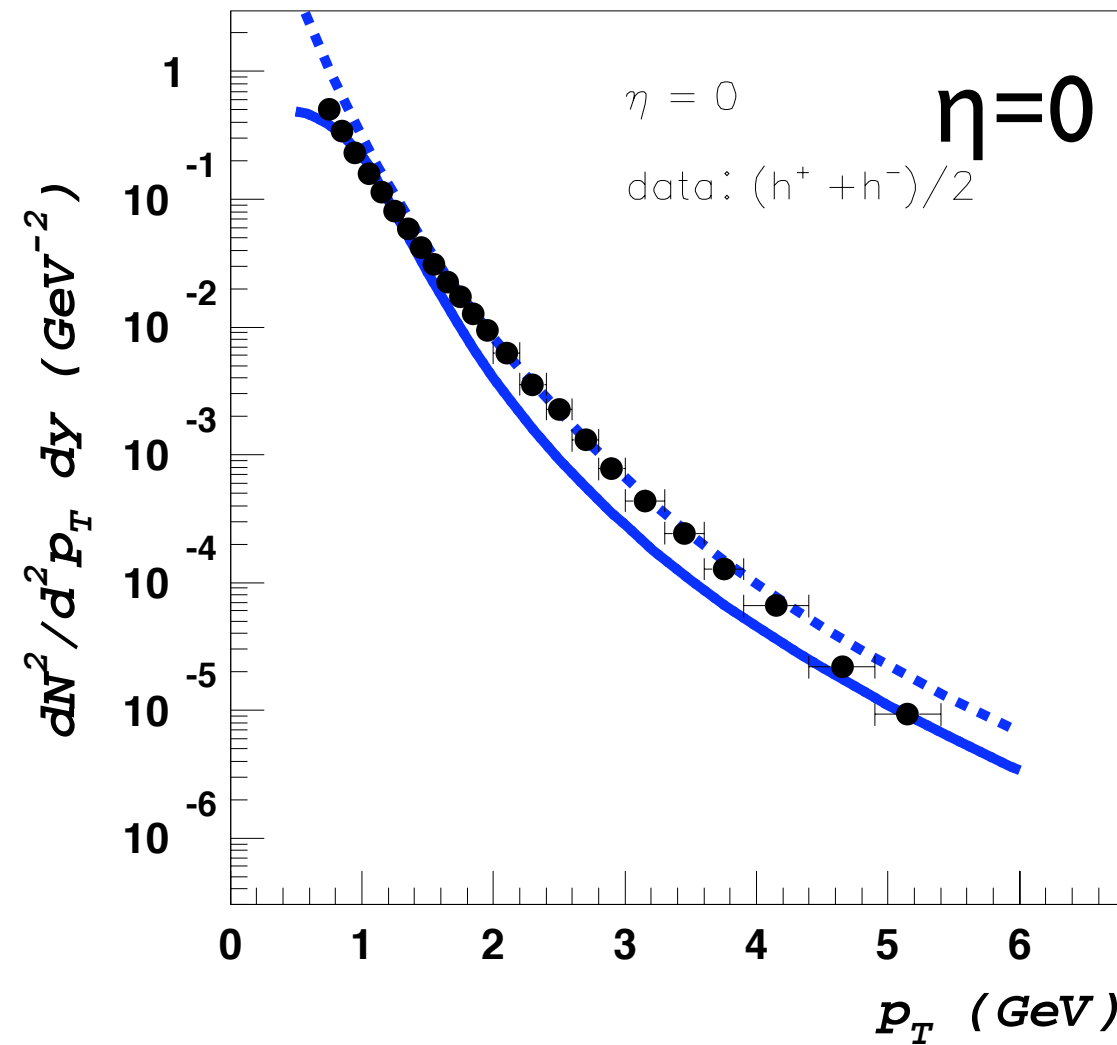
by STAR



# Hadron spectra in dAu

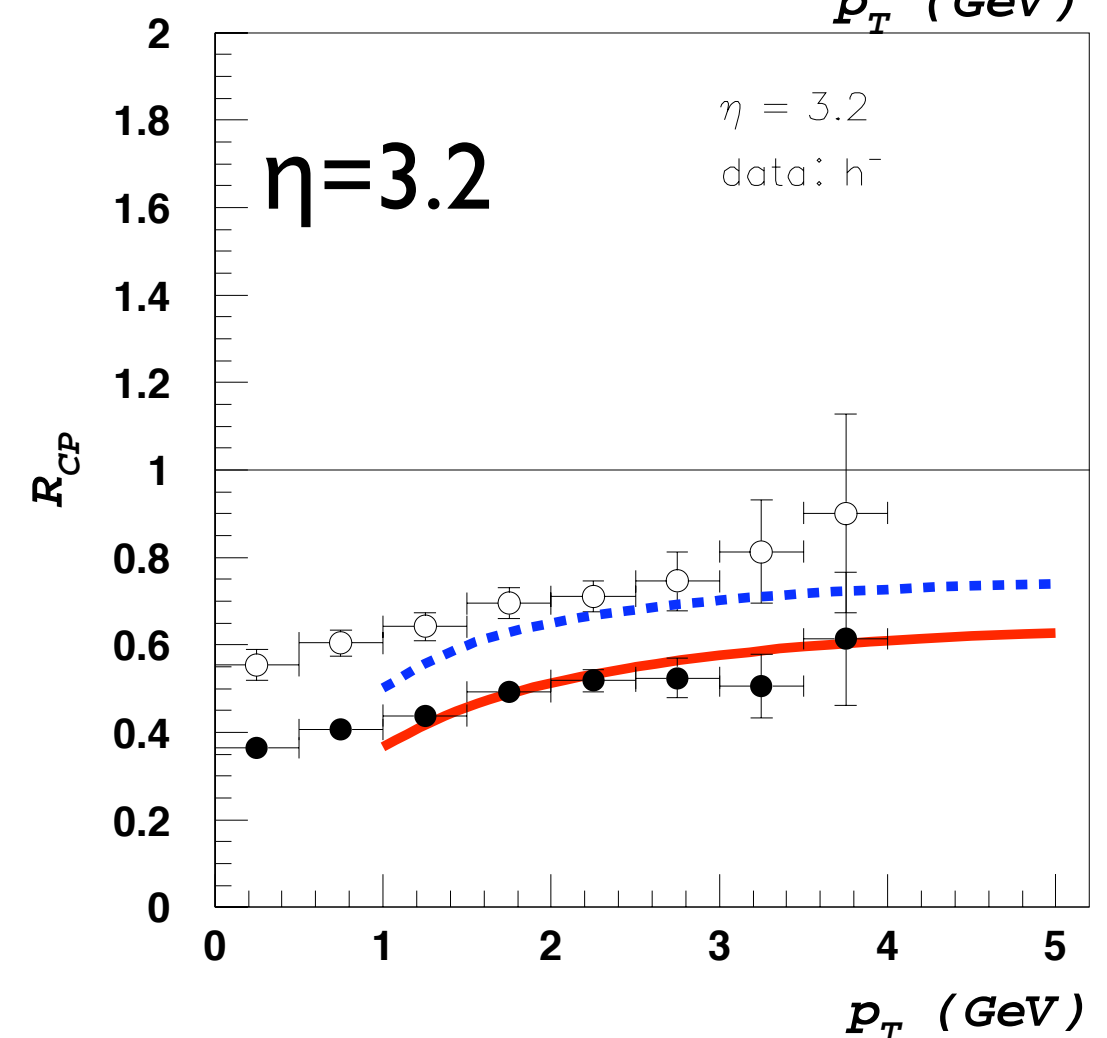
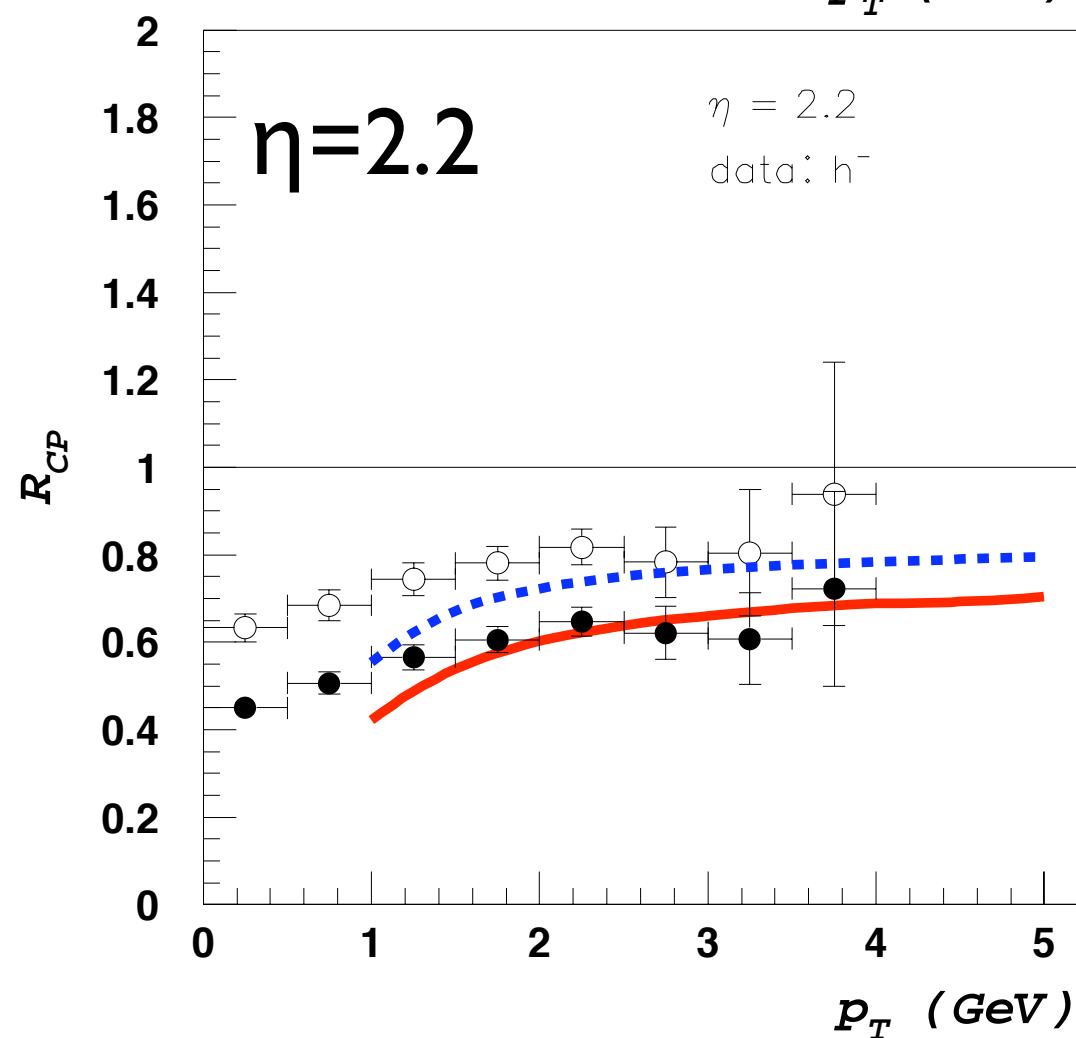
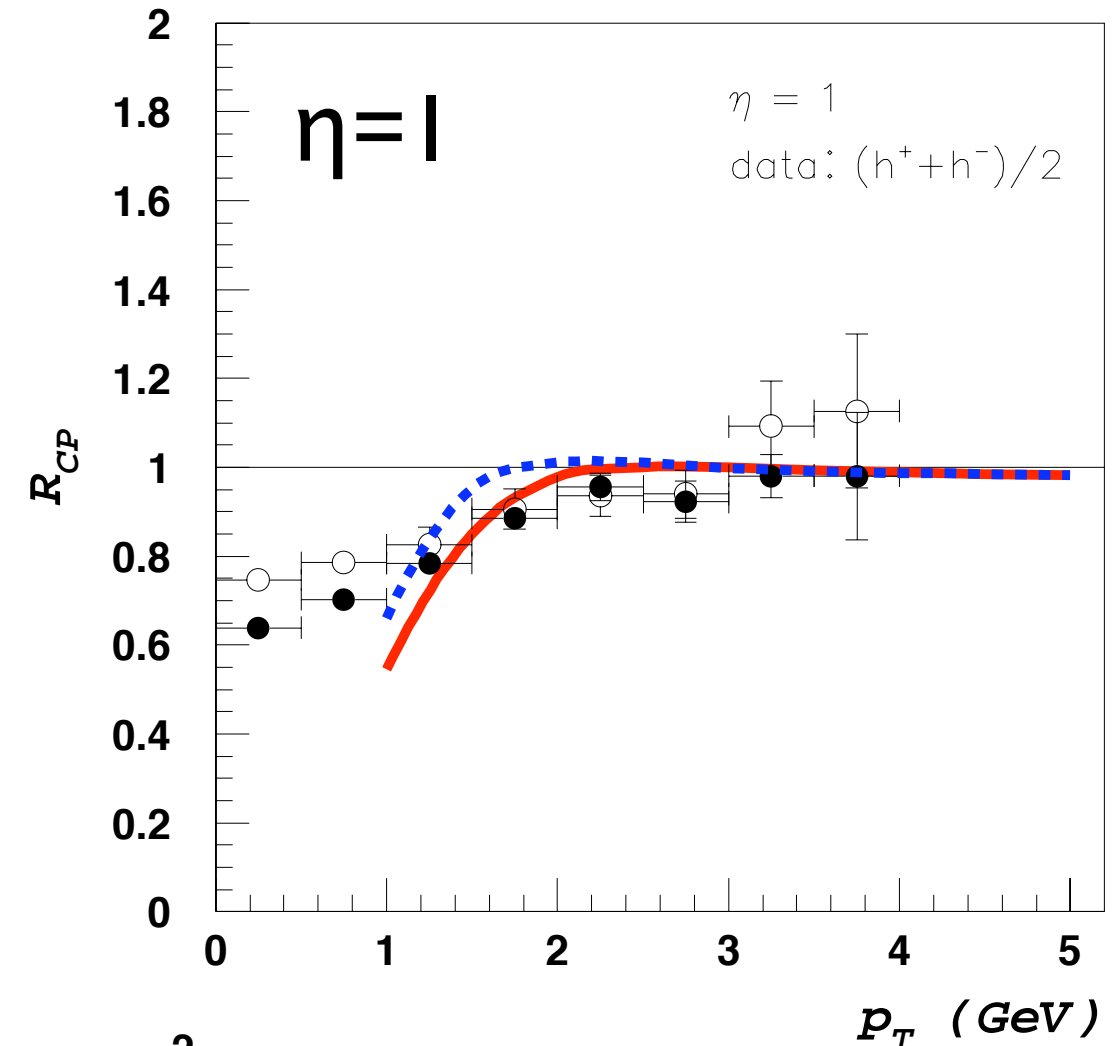
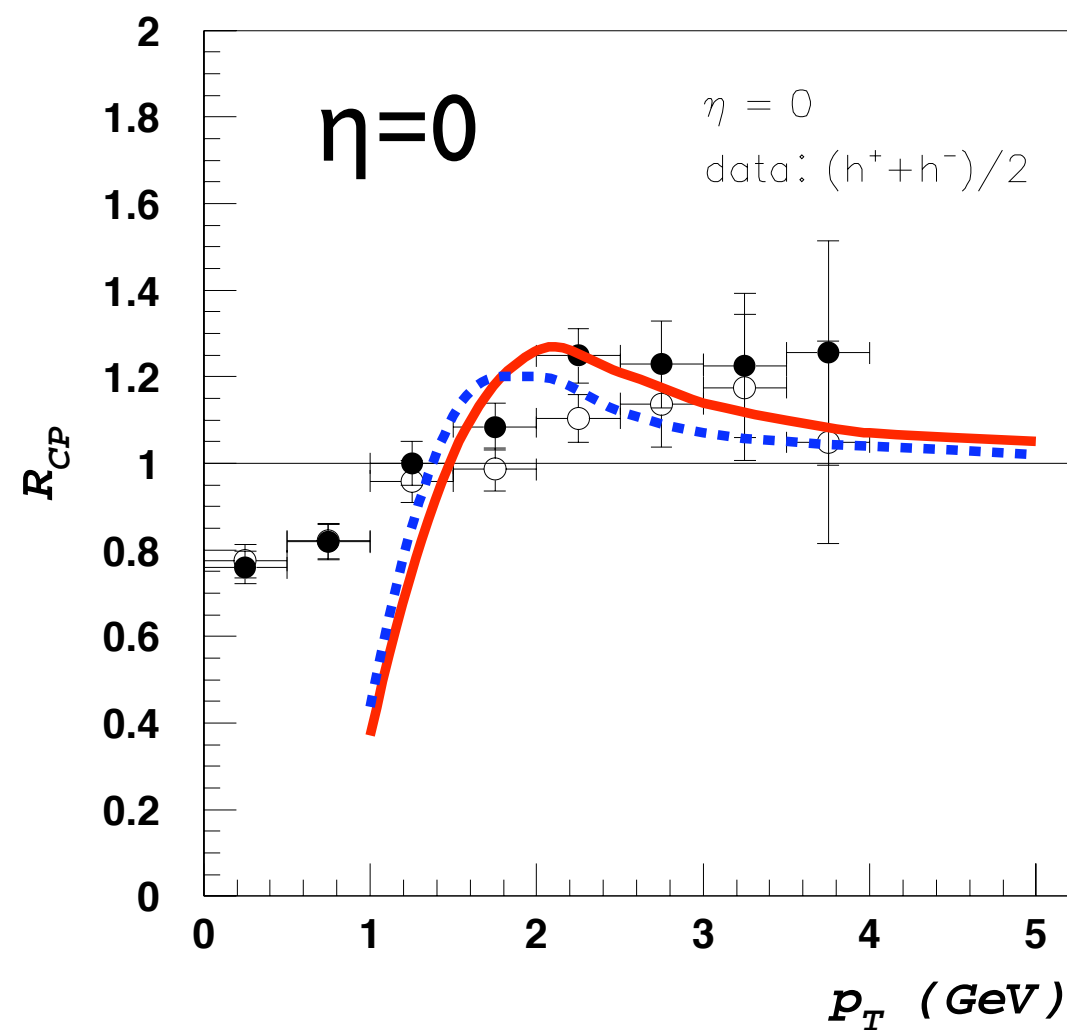
Kharzeev,  
Kovchegov,  
KT

data by  
BRAHMS



# Hadron spectra in dAu

Kharzeev,  
Kovchegov,  
KT



data by  
BRAHMS

see also Baier,  
Kovner, Wiedemann



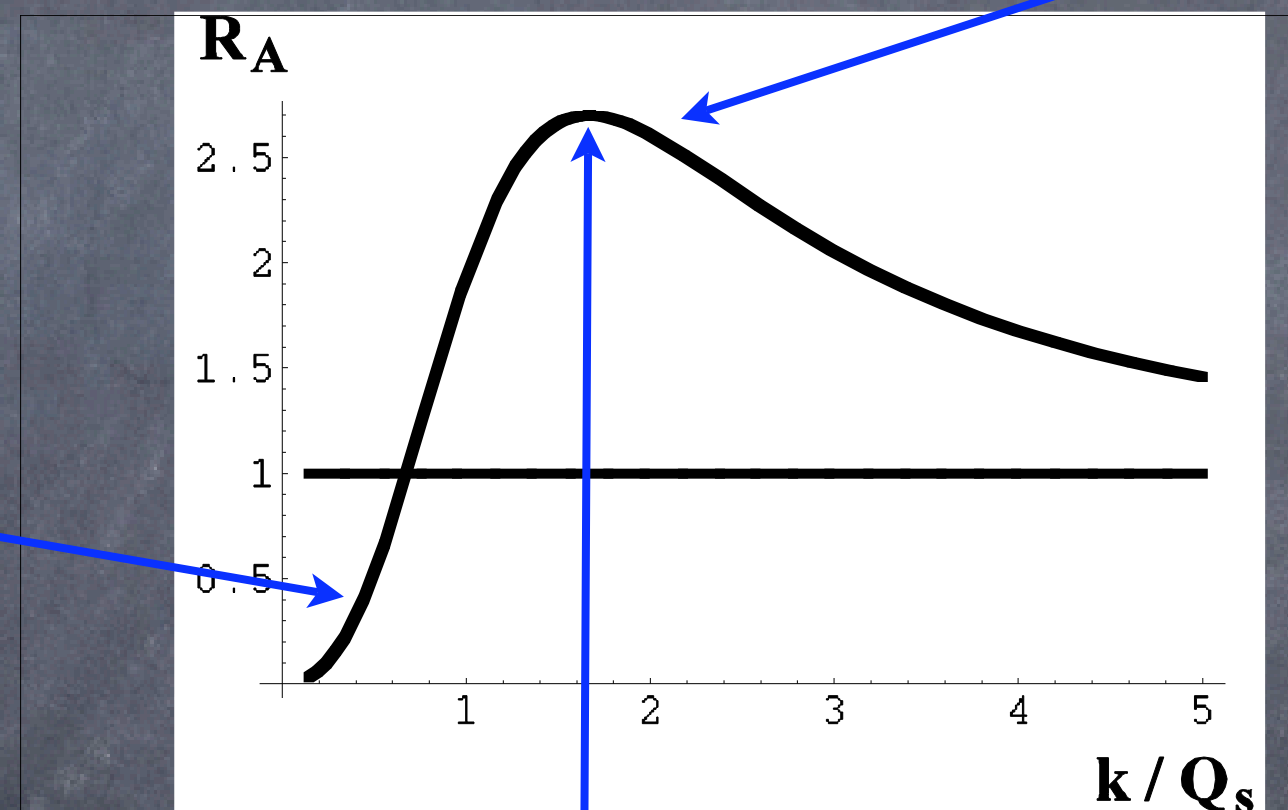
# Physics behind Cronin and suppression

Kharzeev,  
Kovchegov, KT

- In a quasi-classical approximation Cronin enhancement appears due to multiple rescattering of partons in nucleus.

Anti-  
Shadowing

Shadowing:  
small  $k$ , small  $x$



Most gluons are here

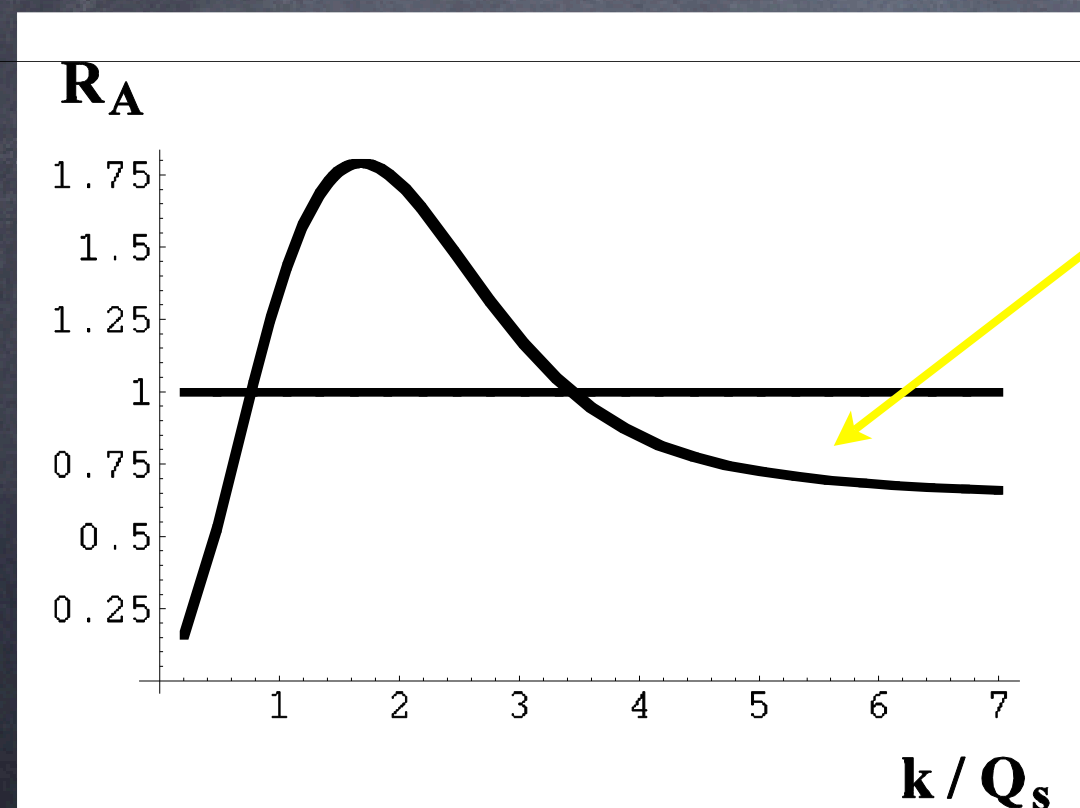
see also  
Baier, Kovner,  
Wiedemann;  
Blaizot, Gelis,  
Venugopalan;  
Iancu, Itakura,  
Triantafyllopoulos

- Gluons are redistributed from low to high  $k_T$

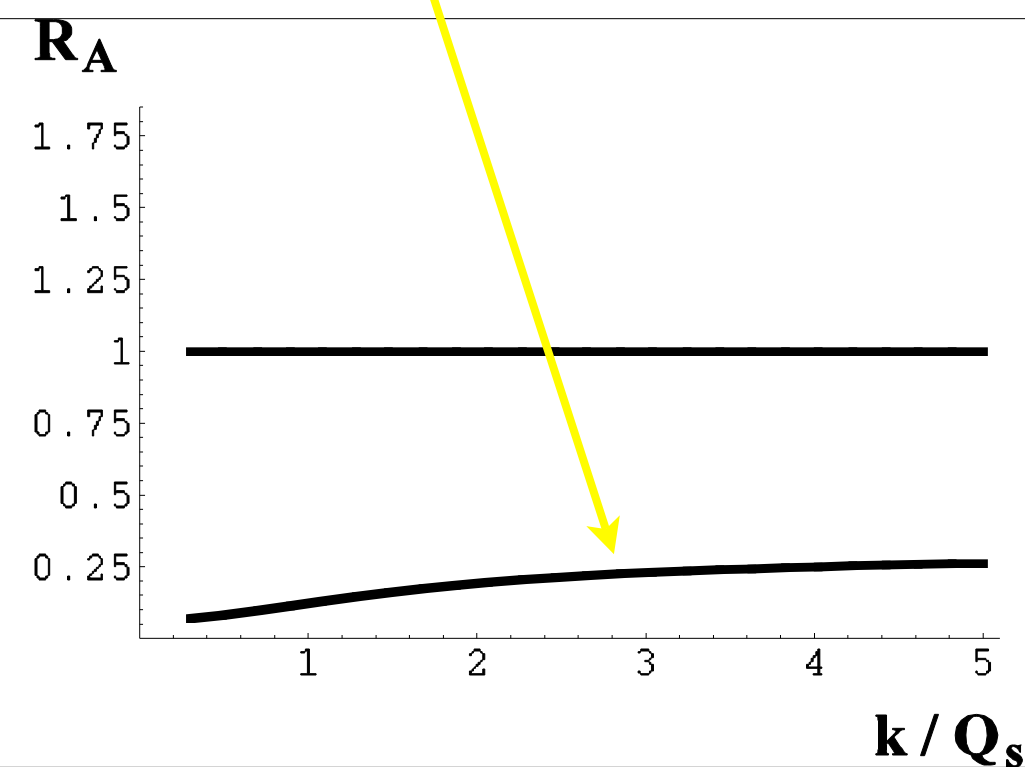
# Physics behind Cronin and suppression

- Due to the non-linear evolution effects at high energies/forward rapidities (low  $x$ ) gluons in dA get stronger suppressed than in pp.

$$\phi(\underline{k}, y) \sim \left( \frac{Q_s^2}{k^2} \right)^\gamma \quad \gamma \approx \frac{1}{2} \Rightarrow \phi \propto A^{1/6} \text{ instead of } A^{1/3}$$



Kharzeev, Levin, McLerran



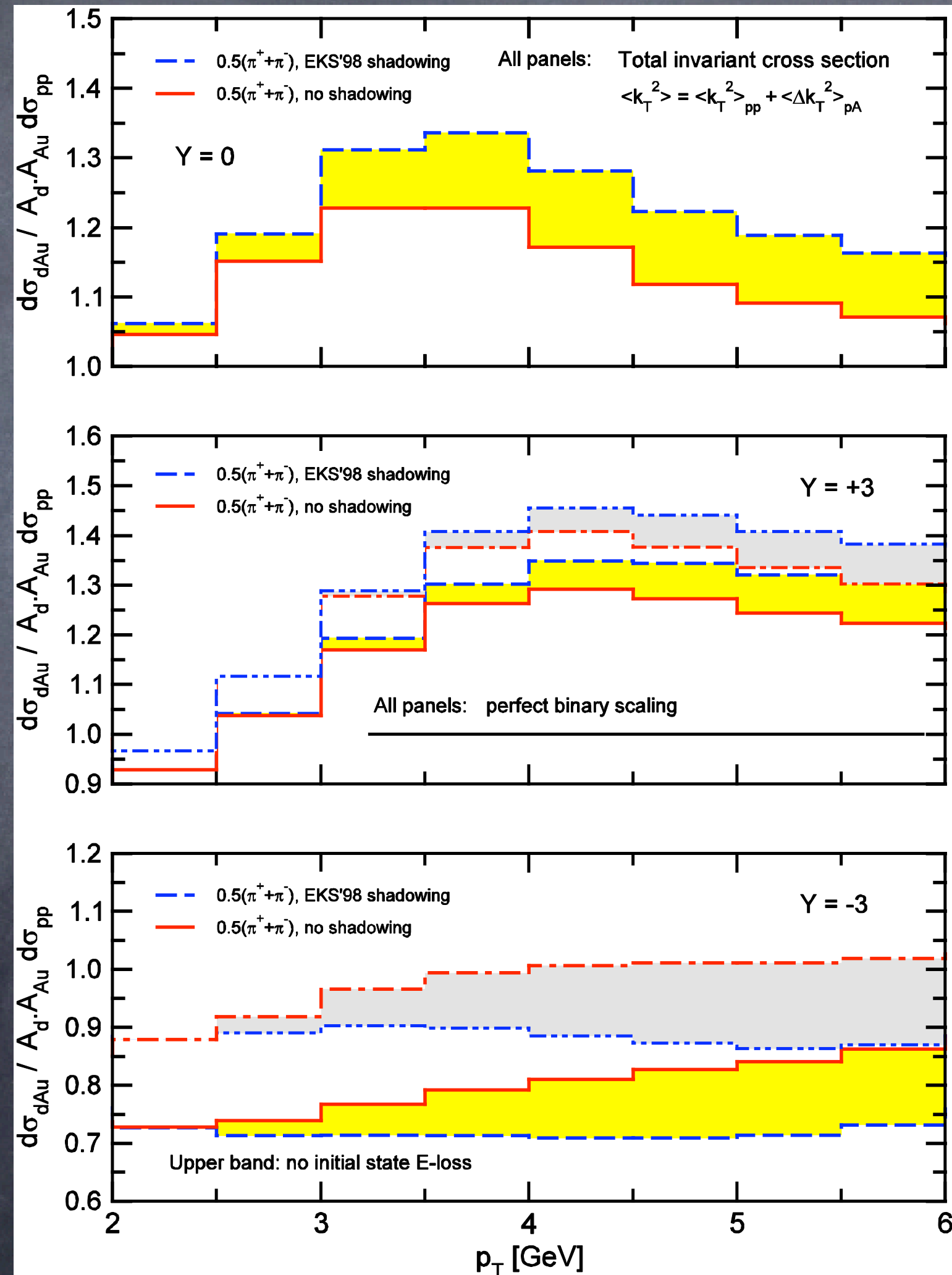
Kharzeev,  
Kovchegov,  
KT

see also  
Baier, Kovner,  
Wiedemann;  
Blaizot, Gelis,  
Venugopalan;  
Iancu, Itakura,  
Triantafyllopoulos



# Other models

Gyulassy,  
Vitev, Wang,  
Zhang



# Fragmentation effect?

Fragmentation  
effect due to large  
 $x_1$  does not depend  
on energy while the  
saturation effect  
does  $\Rightarrow$

Increase dAu  
energy to verify

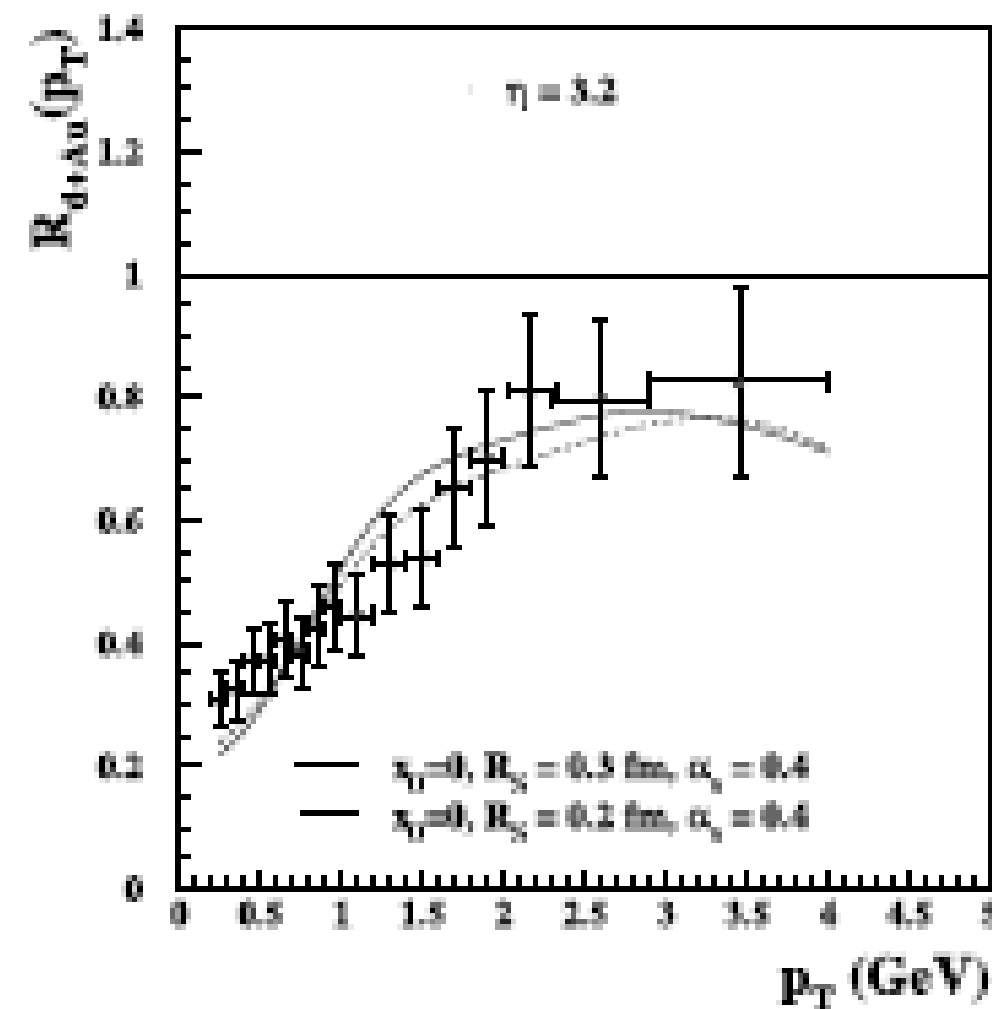


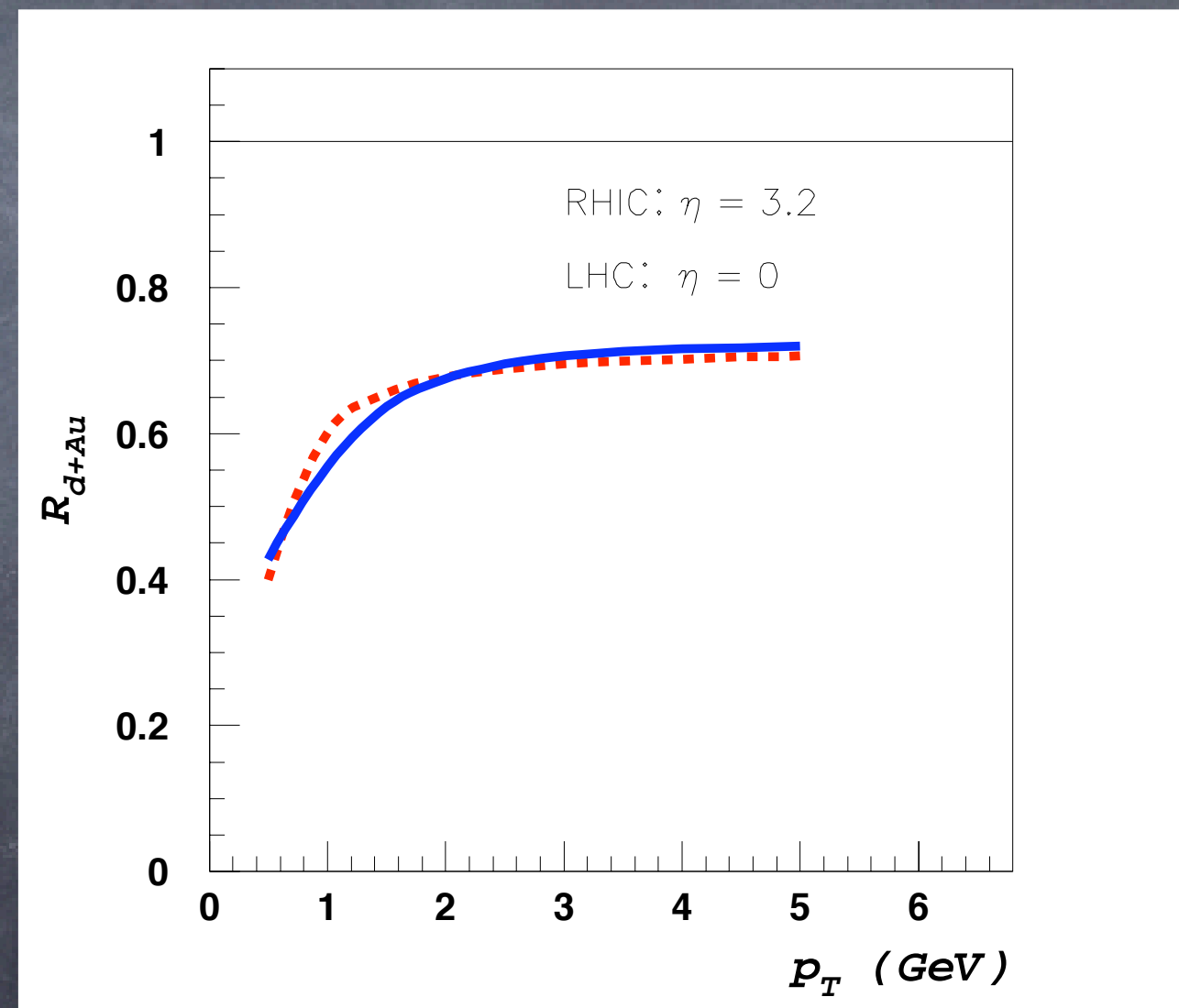
FIG. 3: Ratio of negative particles production rates in  $d - Au$  and  $pp$  collisions as function of  $p_T$ . Data are from [1], solid and dashed curves correspond to calculations with the diquark size 0.3 fm and 0.4 fm respectively.

Kopeliovich et al



# pA at LHC

- Midrapidity at LHC looks similar to  $y \approx 3$  at RHIC.

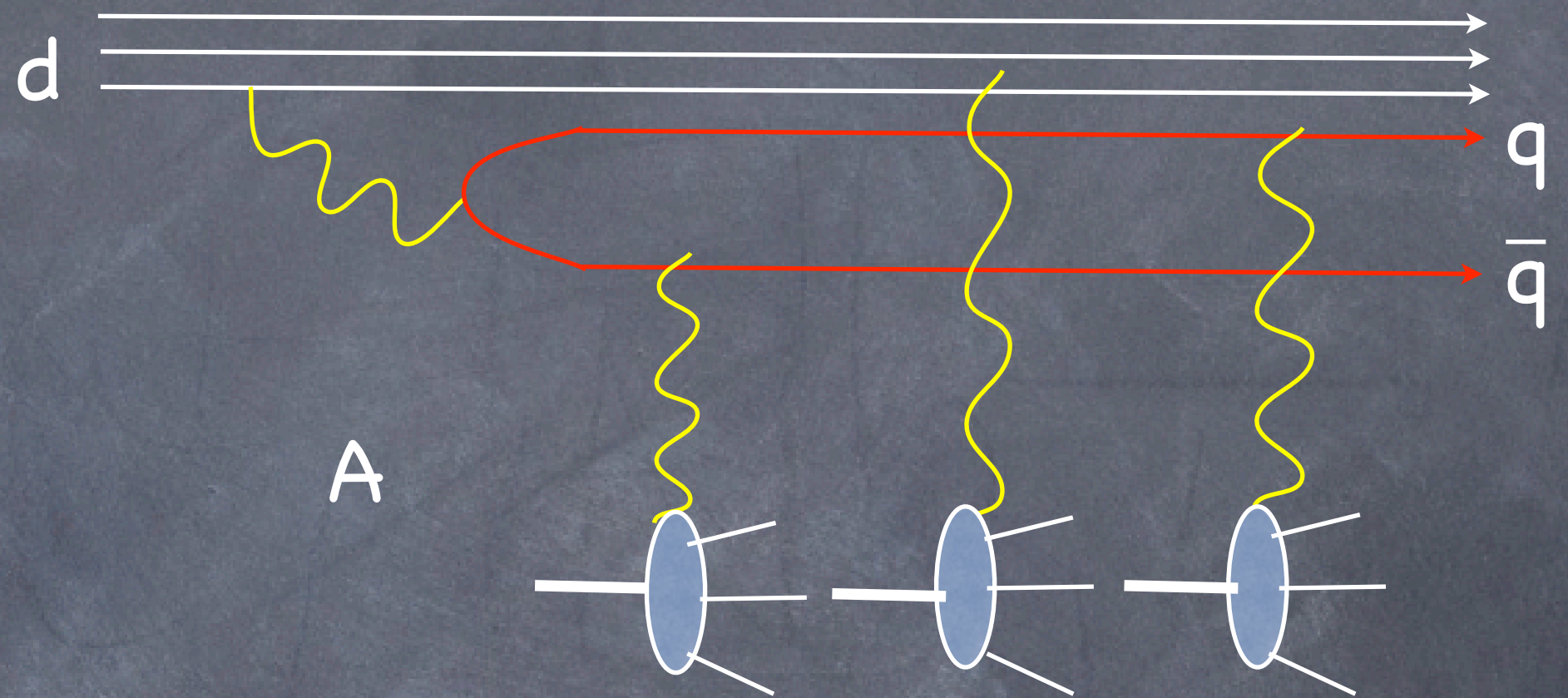


# Heavy Quark Production in pA collisions

- coherence length of qq pair

$$l_c \approx \frac{E_g}{(2m_q)^2} = \frac{1}{2M_N x_2}$$

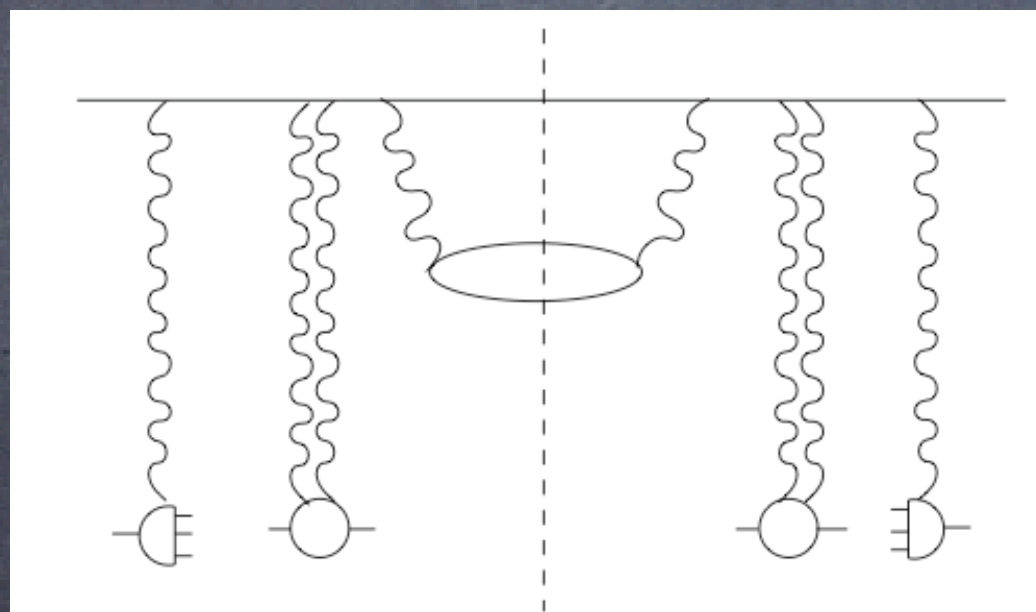
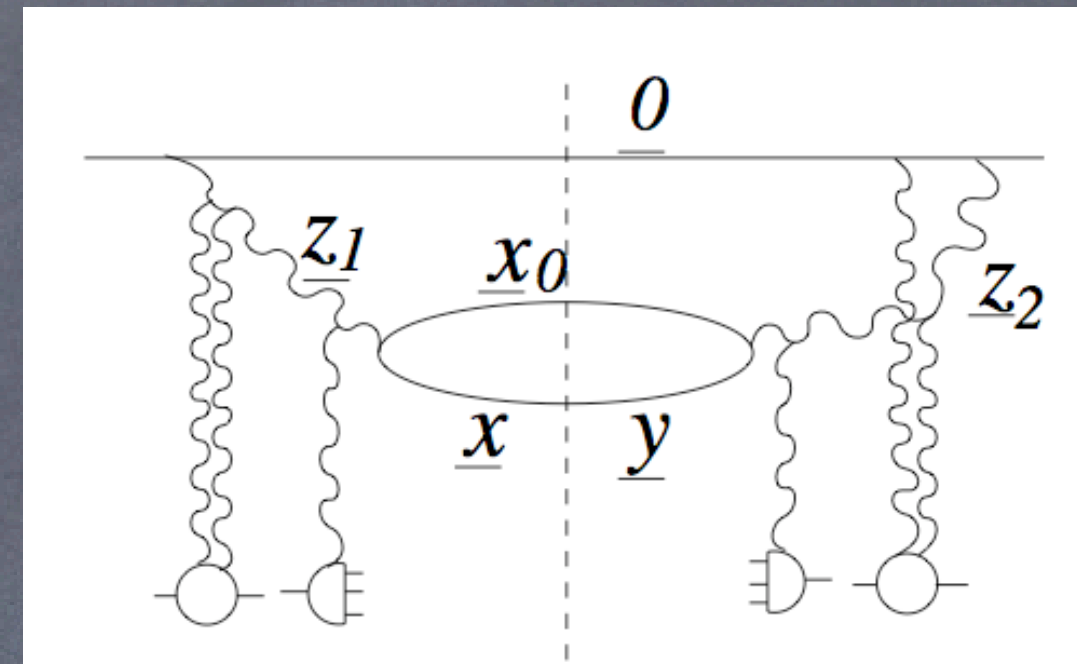
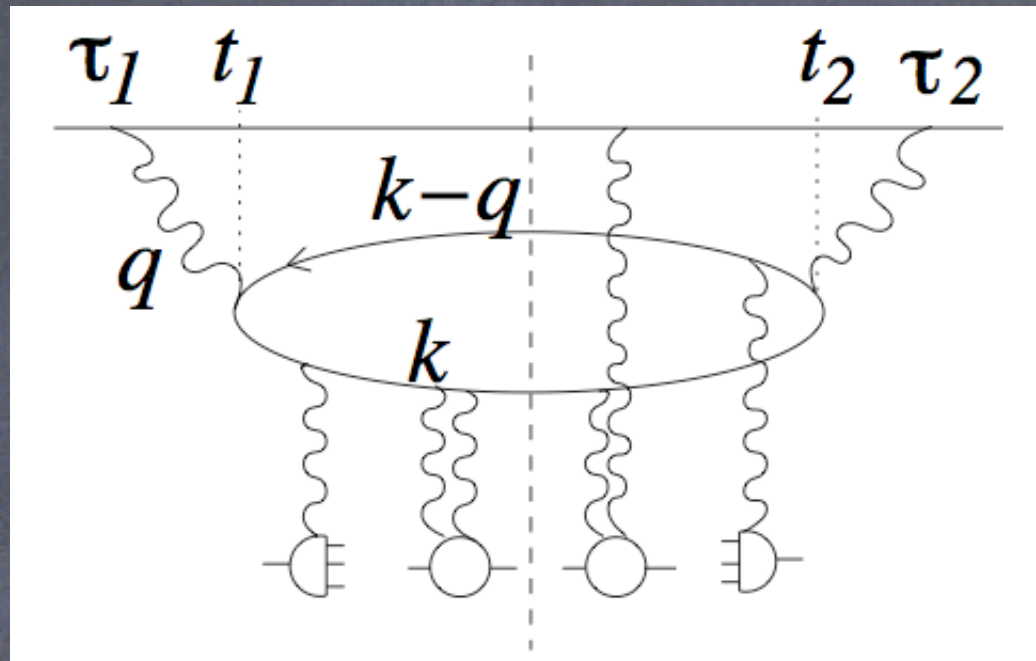
where  $x_2 = \frac{m_T}{\sqrt{s}} e^{-y}$



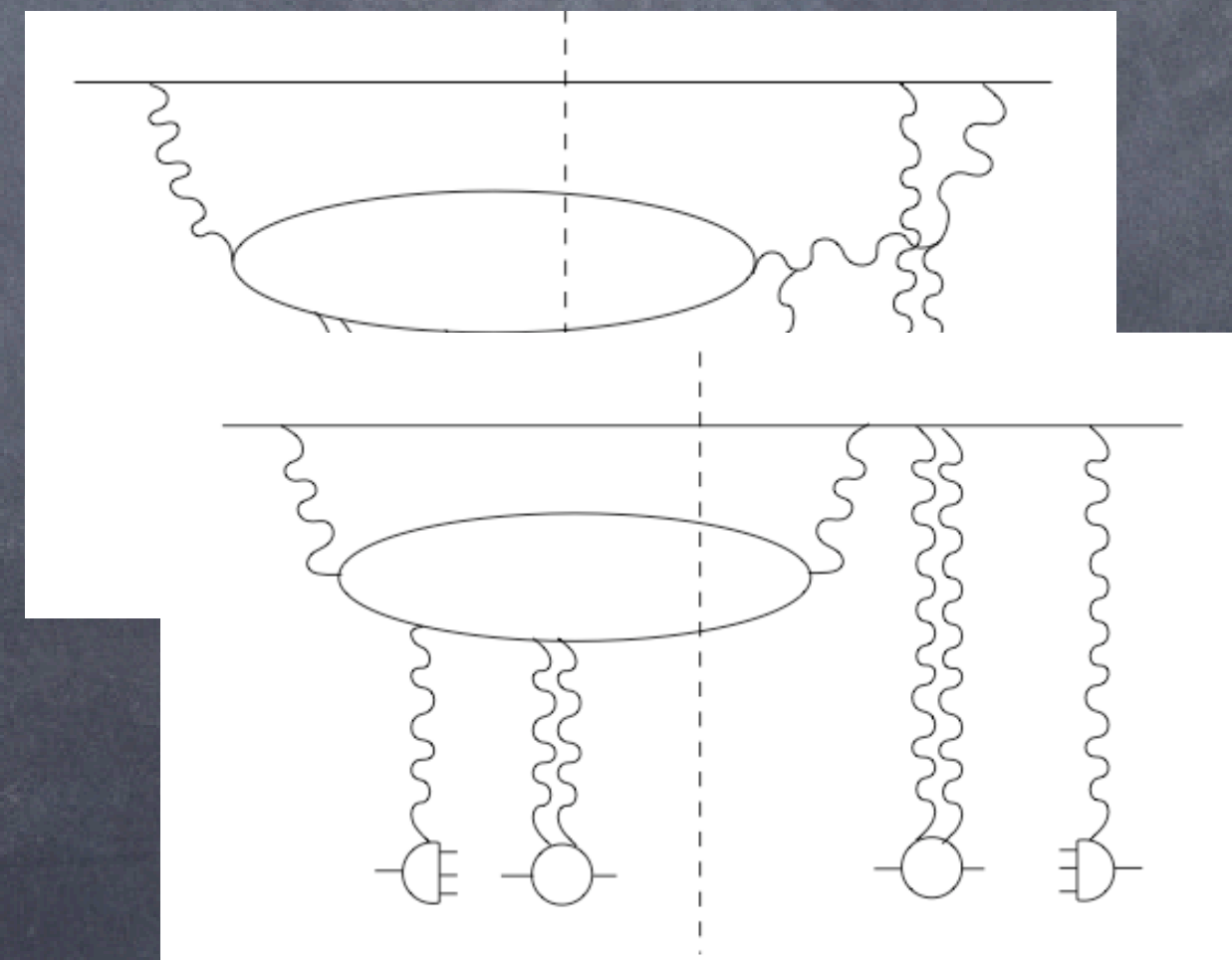
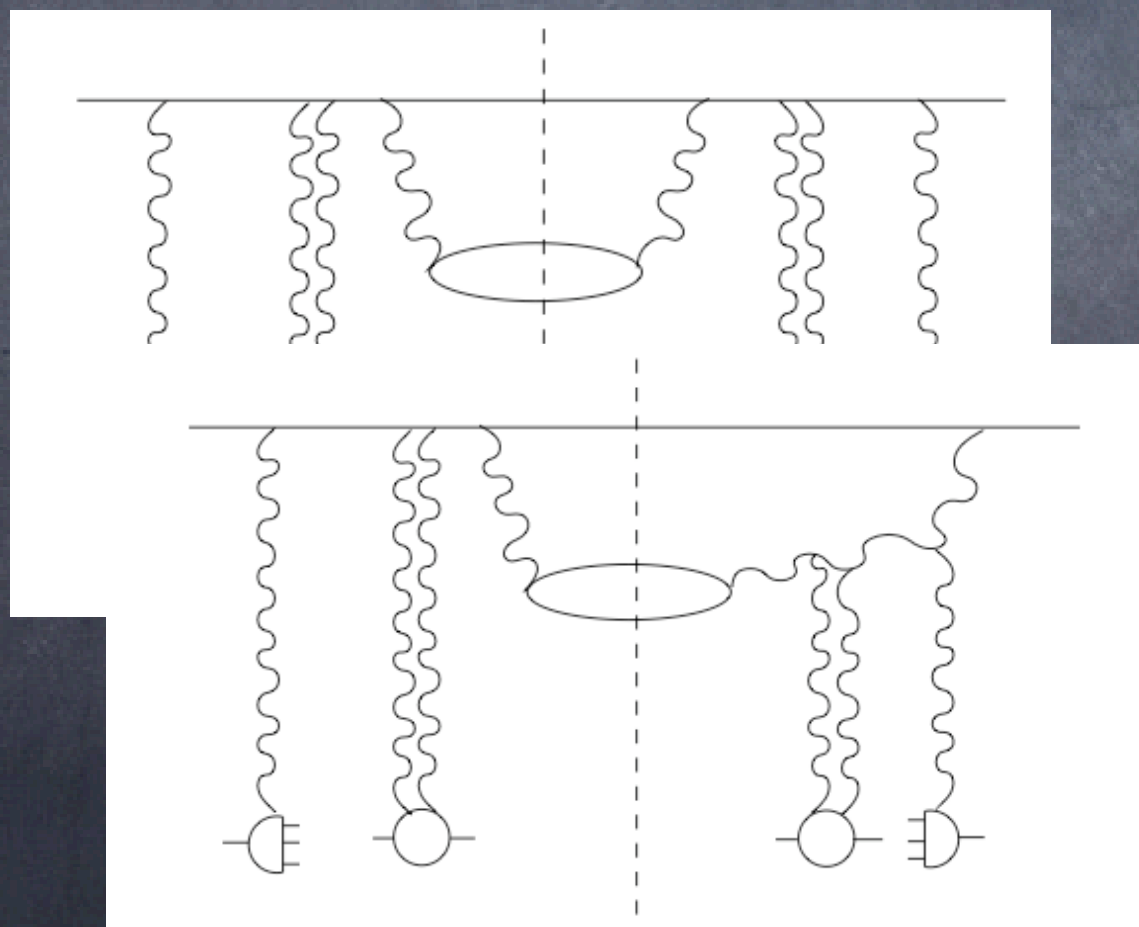
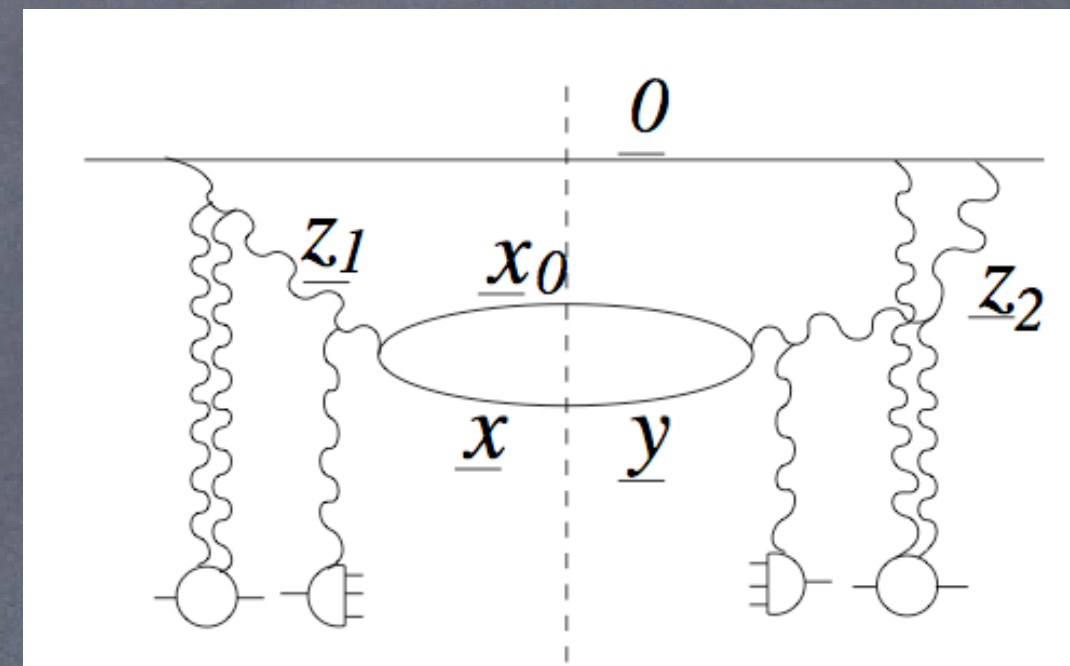
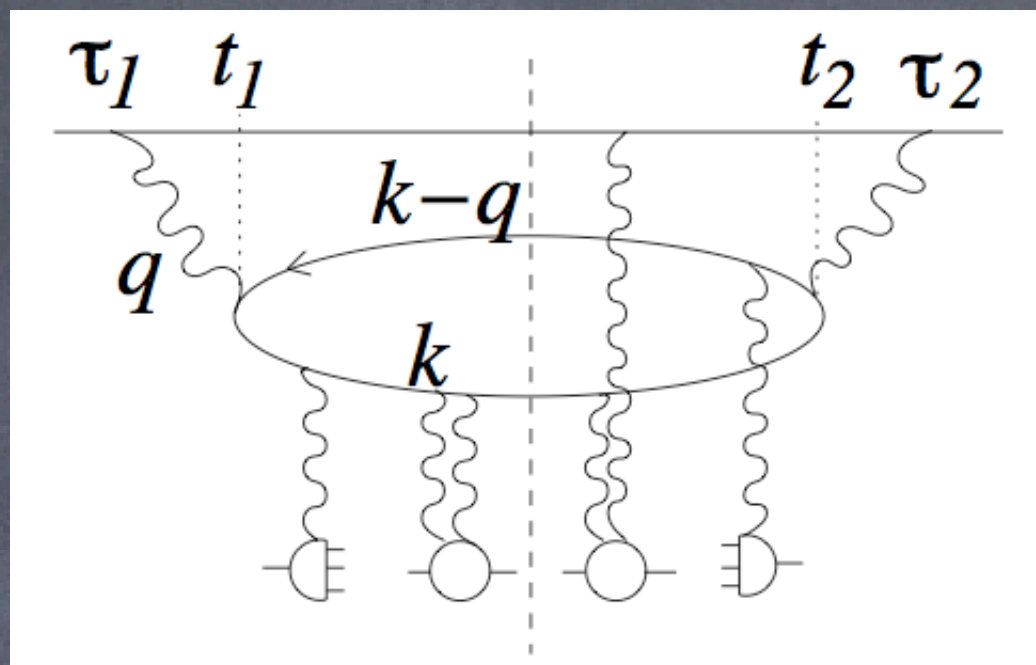
- For charm at RHIC  $l_c = 15e^y$  fm
- At forward rapidity  $l_c \gg R_A$



# Initial vs final state interactions



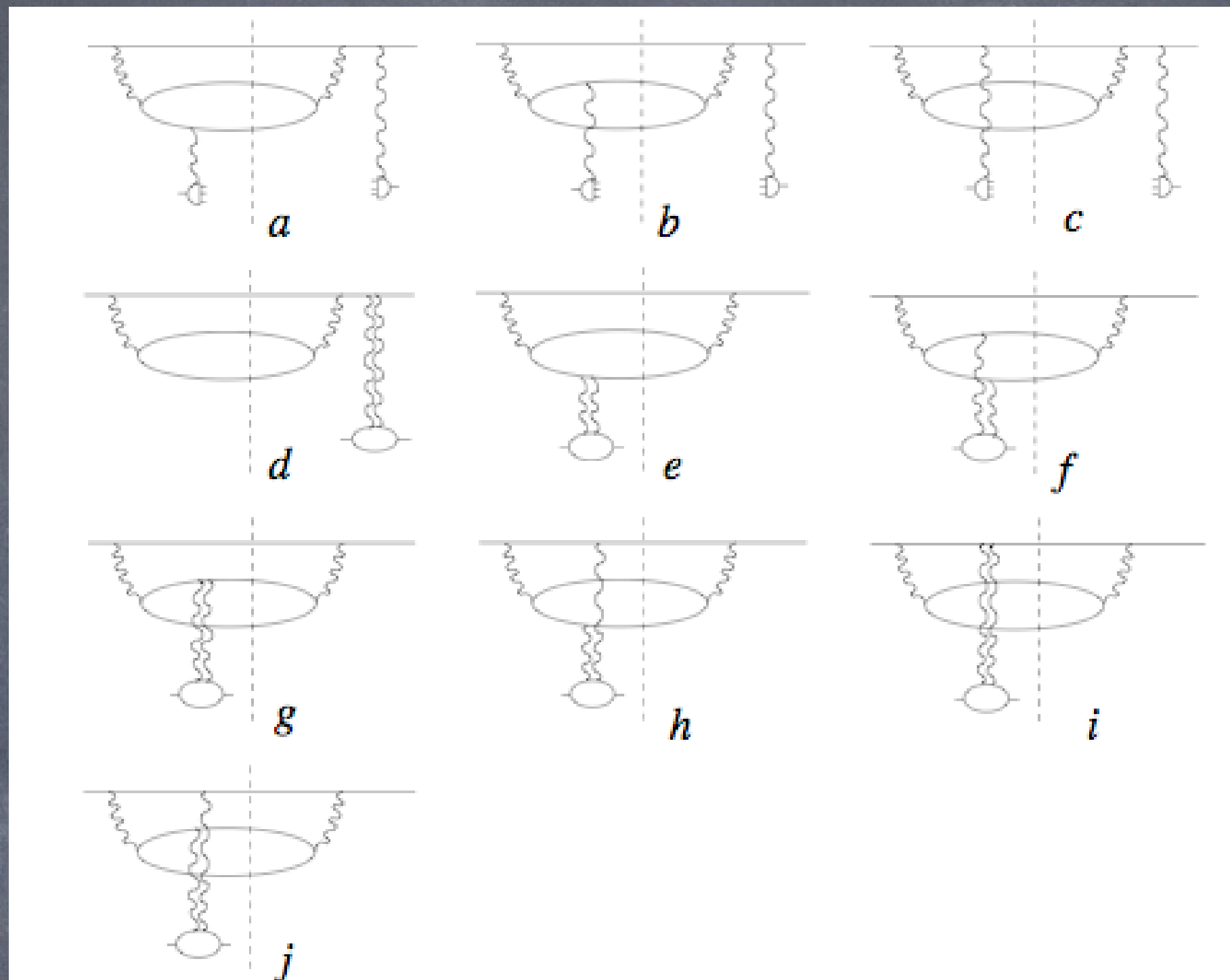
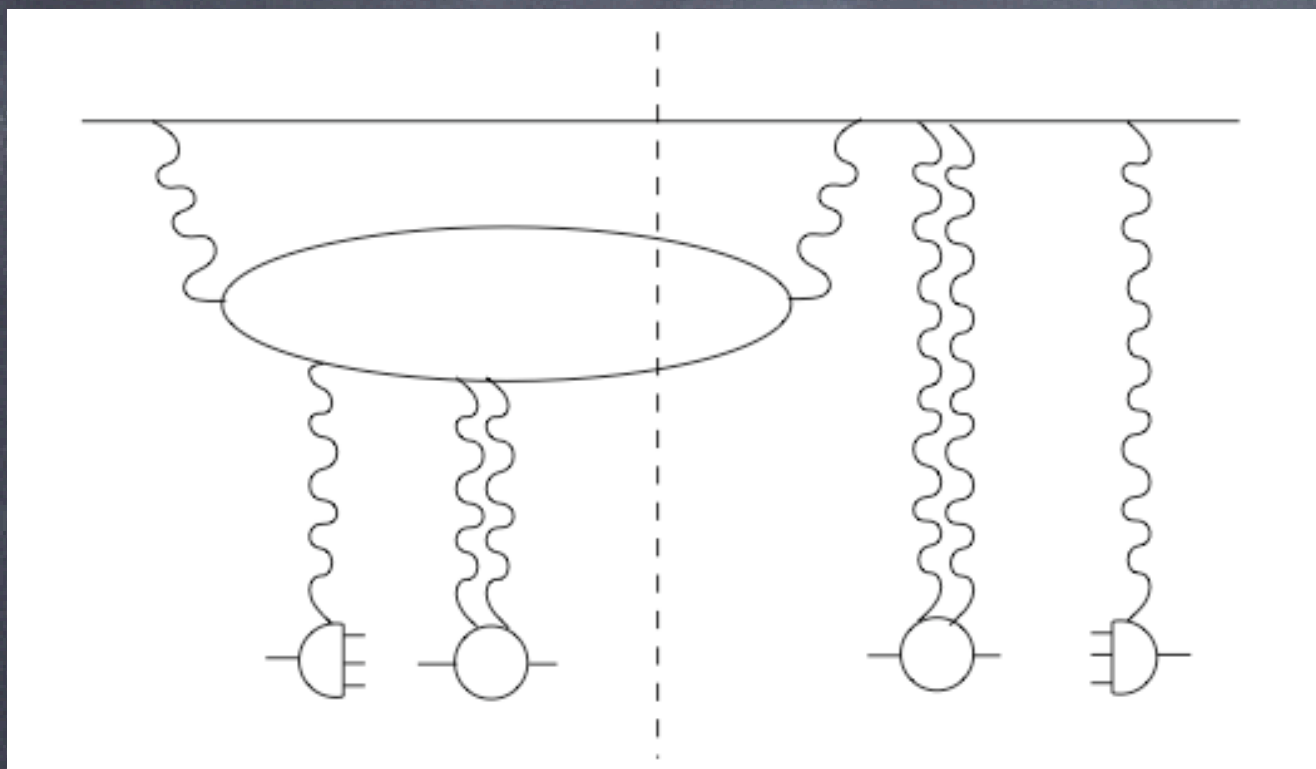
# Initial vs final state interactions





# Dipole-nucleus interactions

- Quasi-classical approximation:



$$-P(\underline{x}, \underline{x}_0) = -\frac{1}{8}\underline{x}^2 Q_s^2 - \frac{1}{8}\underline{x}_0^2 Q_s^2 + \frac{1}{8N_c^2}(\underline{x} - \underline{x}_0)^2 Q_s^2$$

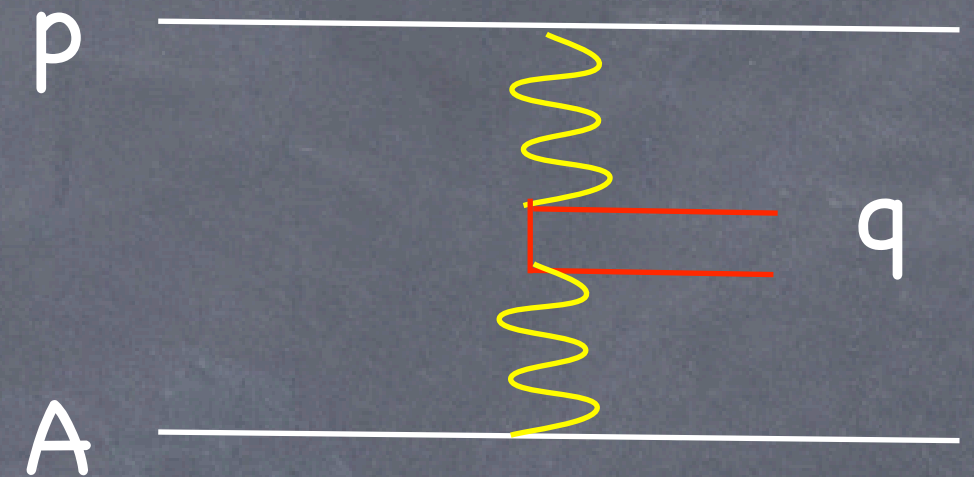
$$Q_s^2 = \frac{2\pi^2 \alpha_s N_c}{C_F} \rho T(\underline{b}) x G(x, 1/\underline{x}^2)$$

see also

Kopeliovich, Tarasov

# Single inclusive quark x-section

KT;  
Kovchegov, KT



Size of the initial dipole

Number of dipoles in proton

Total rapidity Quark rapidity

$$\frac{d\sigma}{d^2k dy_1 dy_2}(z_{01}) = \frac{1}{2(2\pi)^4} \int d^2z'_0 d^2z'_1 n_1(\underline{z}_0, \underline{z}_1; \underline{z}'_0, \underline{z}'_1; Y - y) d^2x_1 d^2x_2 d^2y_1 e^{-i\underline{k} \cdot (\underline{x}_1 - \underline{y}_1)} \\ \times \int_0^1 d\alpha \sum_{i,j=1}^3 \sum_{k,l=0}^1 (-1)^{k+l} \Phi_{ij}(\underline{x}_1 - \underline{z}_k, \underline{x}_2 - \underline{z}_k; \underline{y}_1 - \underline{z}_l, \underline{x}_2 - \underline{z}_l; \alpha) \Xi_{ij}(\underline{x}_1, \underline{x}_2, \underline{z}_k; \underline{y}_1, \underline{x}_2, \underline{z}_l; \alpha, y)$$

qq wave functions for different time orderings

Rescattering factors

see also Blaizot,  
Gelis, Venugopalan



# Aligned jet configuration

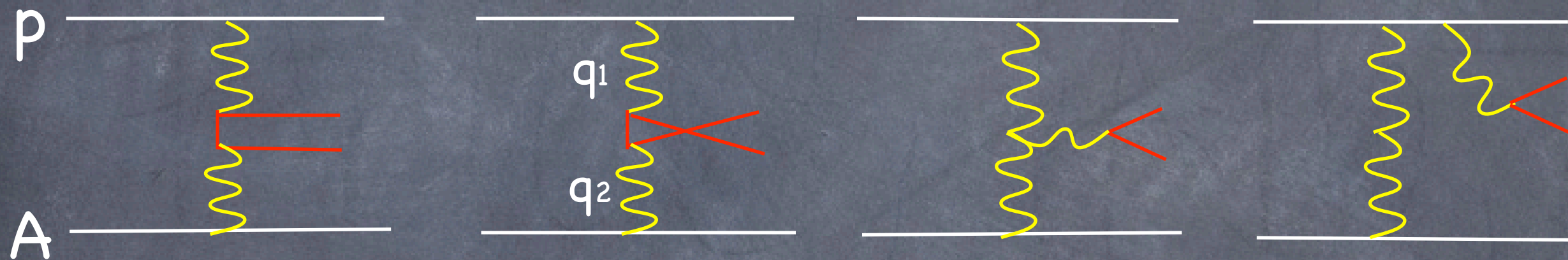
KT

- Assume that quark energy  $\gg$  anti-quark energy
- Then,  $l_c(G) \gg l_c(q\bar{q}) \gg R_A$
- Gluon emission and pair production factorize: the light cone wave function  $= \psi_G \otimes \psi_{qq}$
- Although the quark production x-section is quite simple in this case (only 7-dim integral :) it applies only in the situation when  $q$  and anti- $q$  are separated by large rapidity gap.
- Exact result: see Kovchegov, KT, 06

# $k_T$ -factorization

Levin, Ryskin, Shabelsky, Shuvaev,  
Catani, Ciafaloni, Hautmann,  
Collins, Ellis  
All:1991

- $k_T$ -factorization assumes that  $q\bar{q}$  production process can be factorized out from the wave functions of proton and nucleus



- Cross section is much easier to calculate

$$\frac{d\sigma}{d^2k dy_1 dy_2} = \int d^2q_1 \int d^2q_2 \phi_p(\underline{q}_1, y_1) A_{gg}(s, t, u, q_1, q_2) \phi_A(q_2, y_2)$$

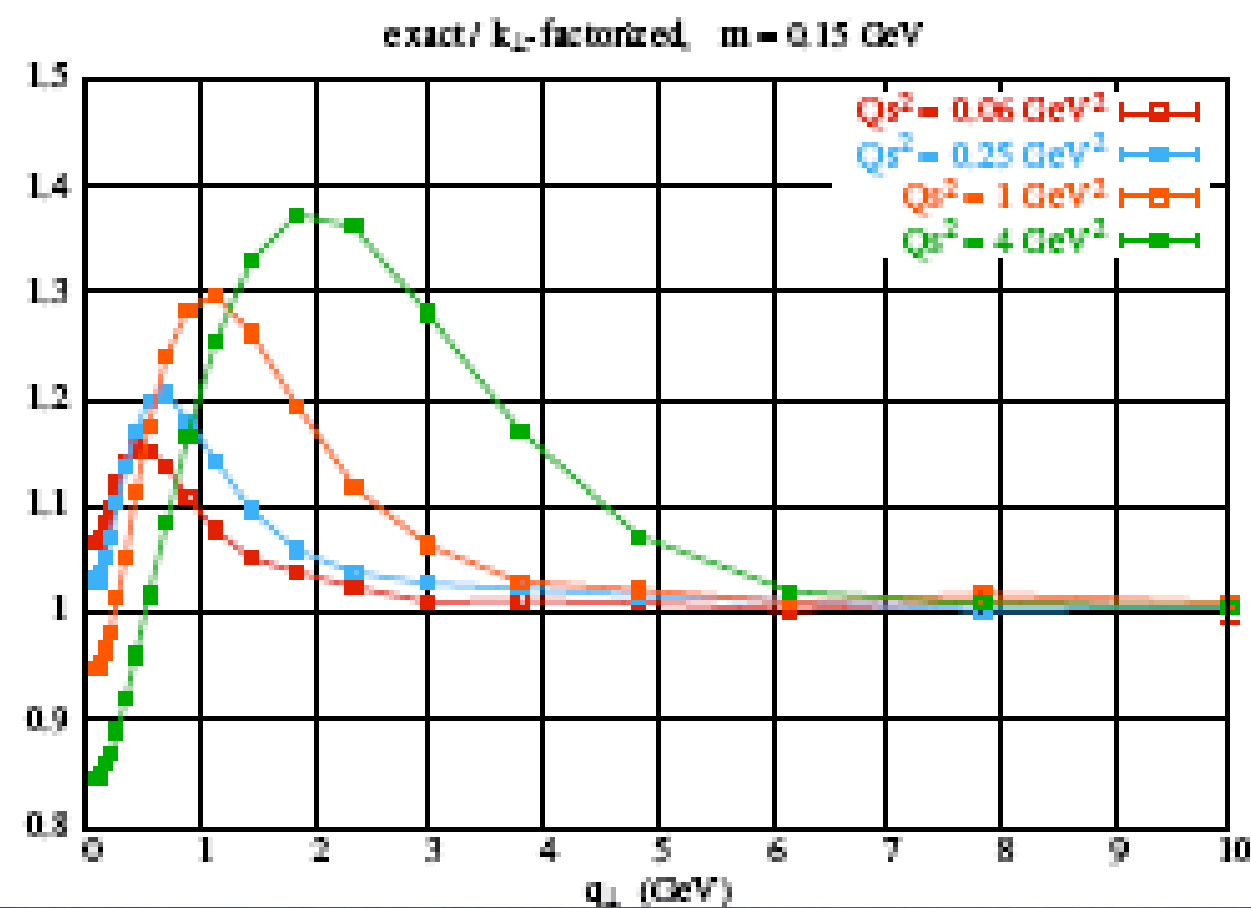
- It was proved for single inclusive gluon production in pA (Kovchegov, K.T.);



# How good is $k_T$ -factorization?

Fujii, Gelis, Venugopalan

- Ratio of the BGV result to the  $k_T$ -factorization:

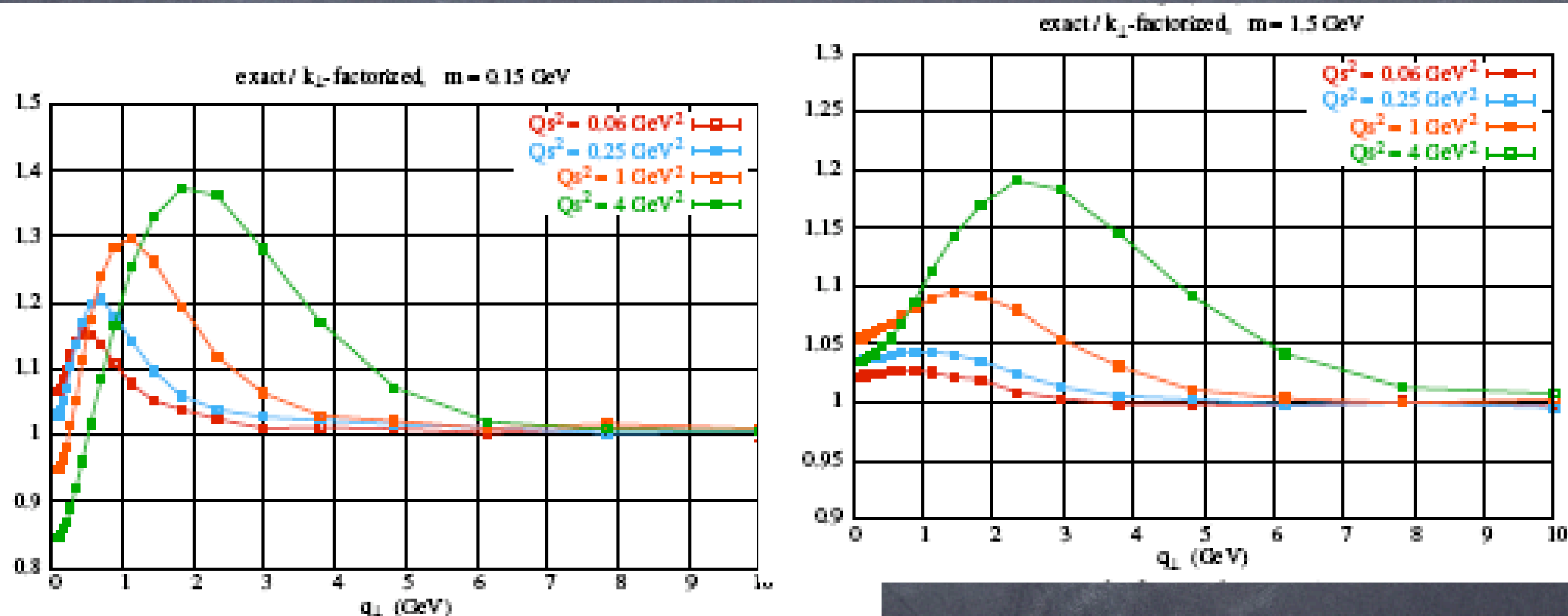




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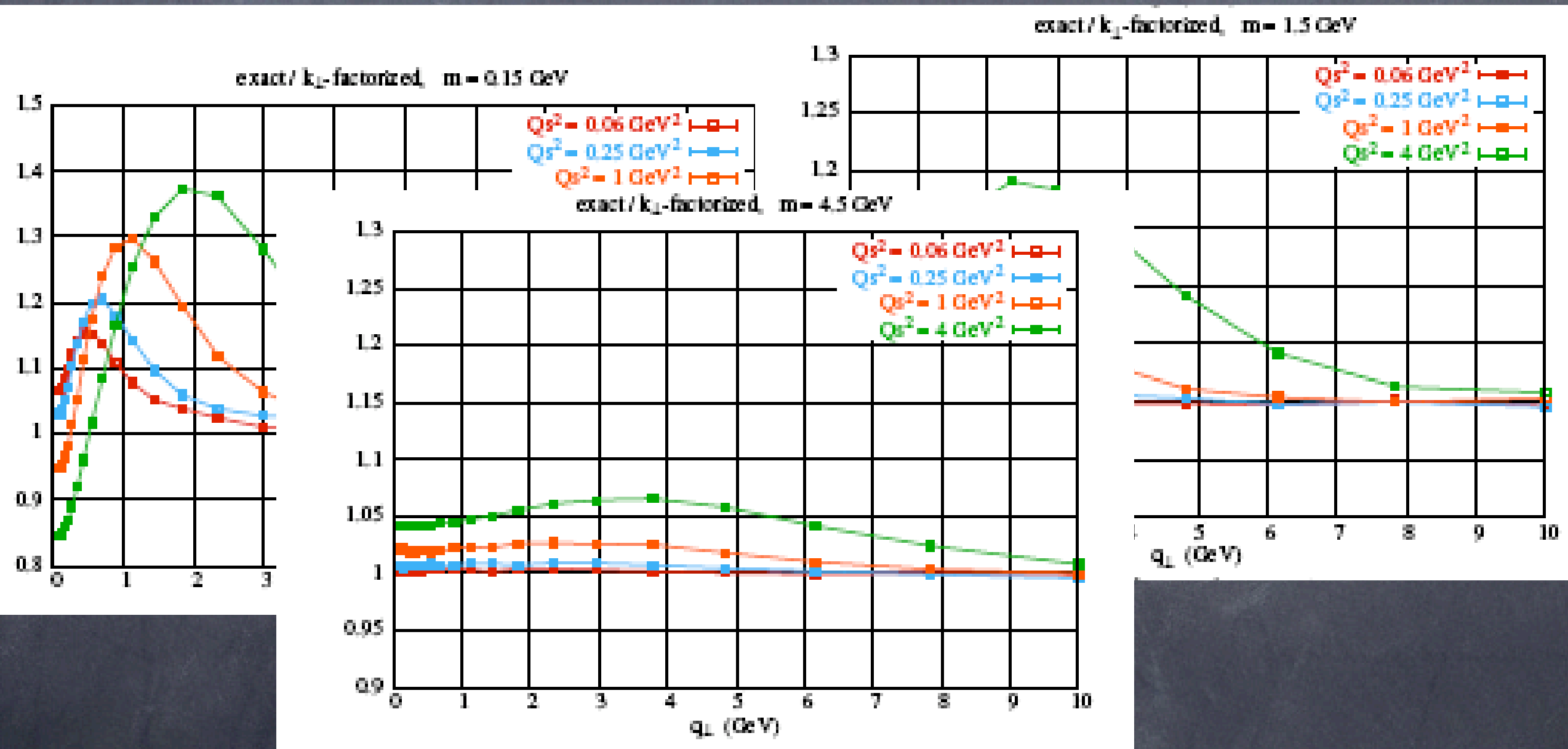
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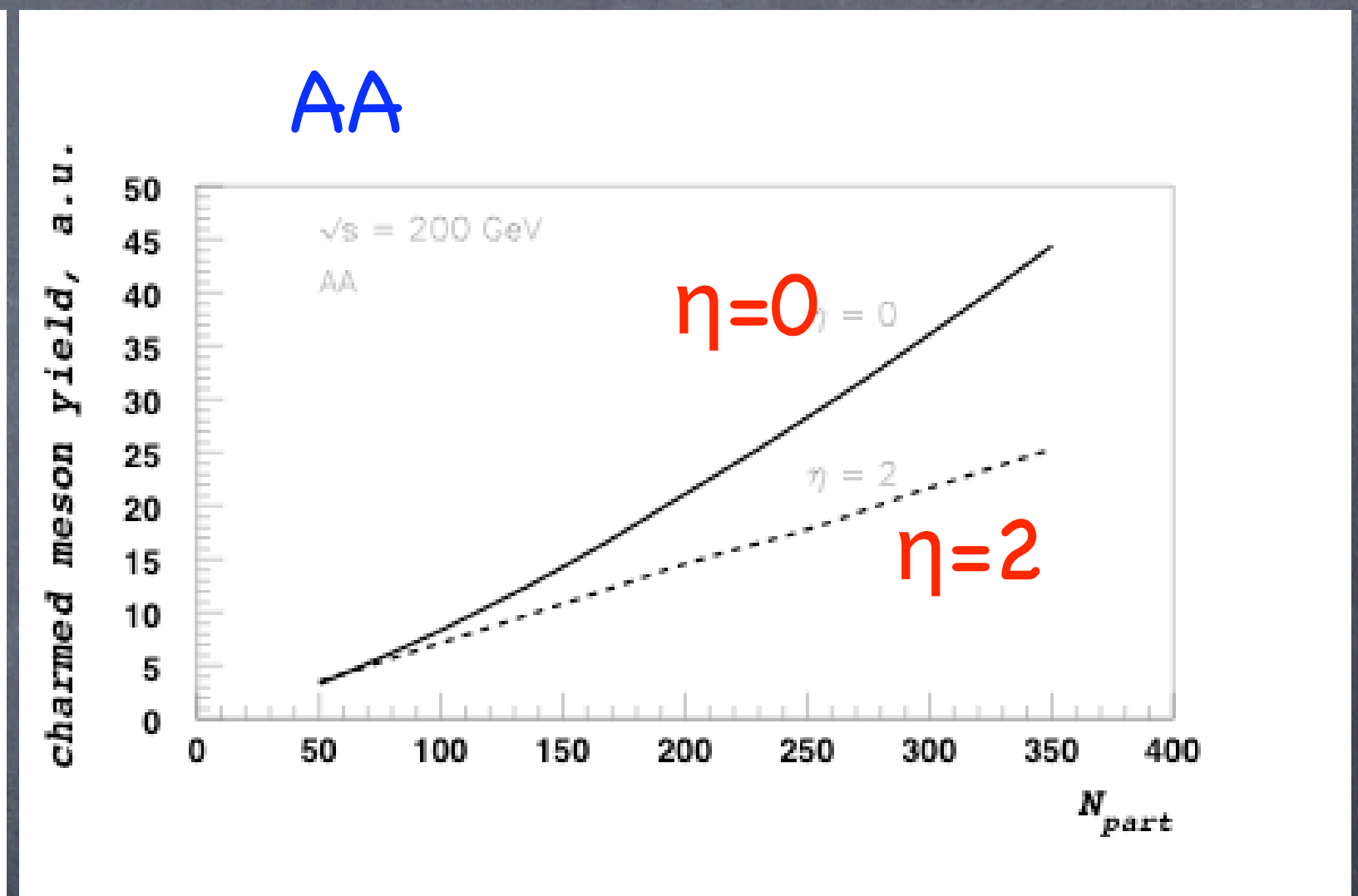
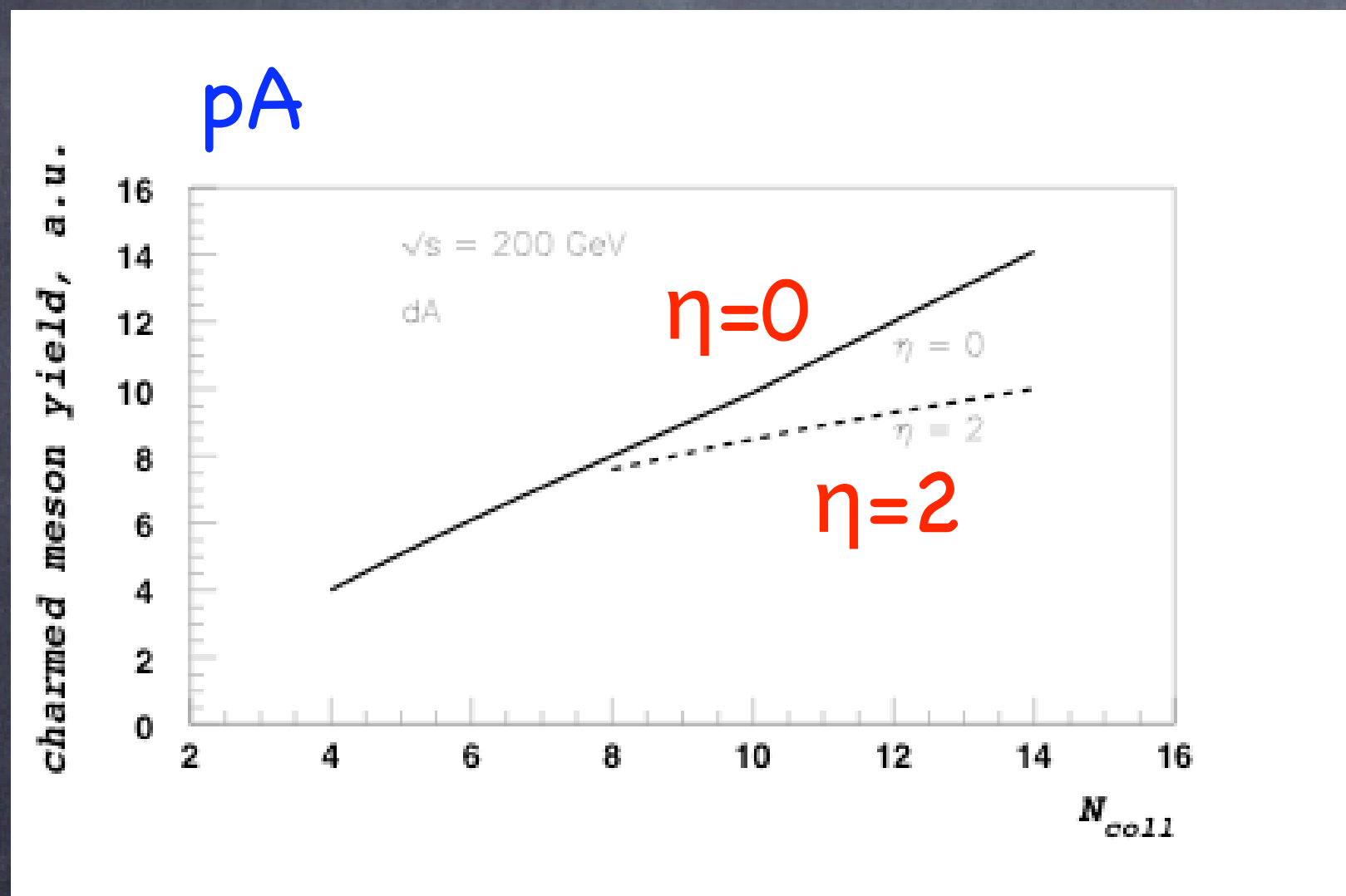
- Ratio of the BGV result to the  $k_T$ -factorization:



# Application to RHIC phenomenology

Kharzeev, KT

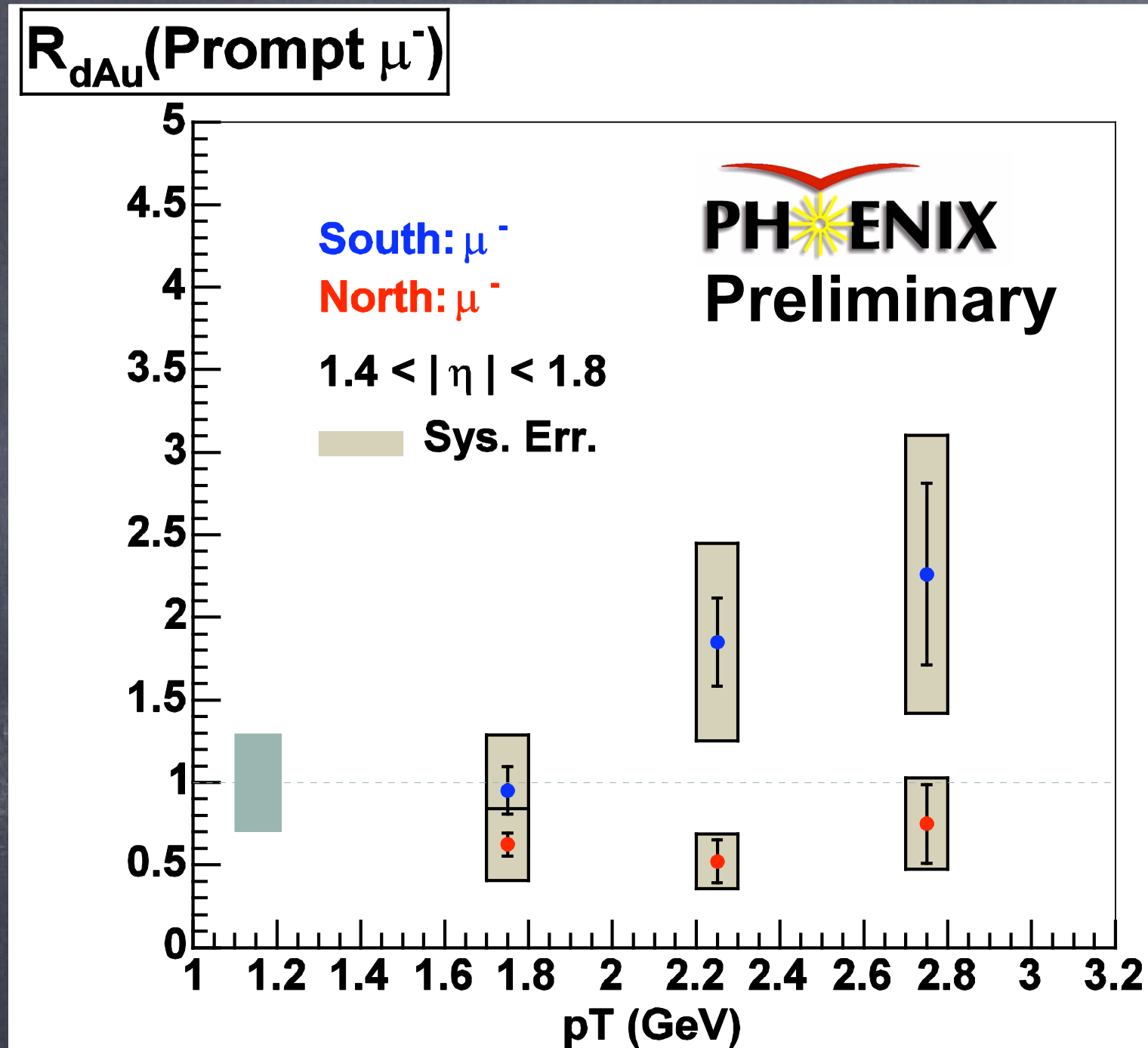
- A model based on  $k_T$ -factorization



- Suppression onsets when  $Q_s > m$ . Production pattern of light and heavy quarks becomes the same.

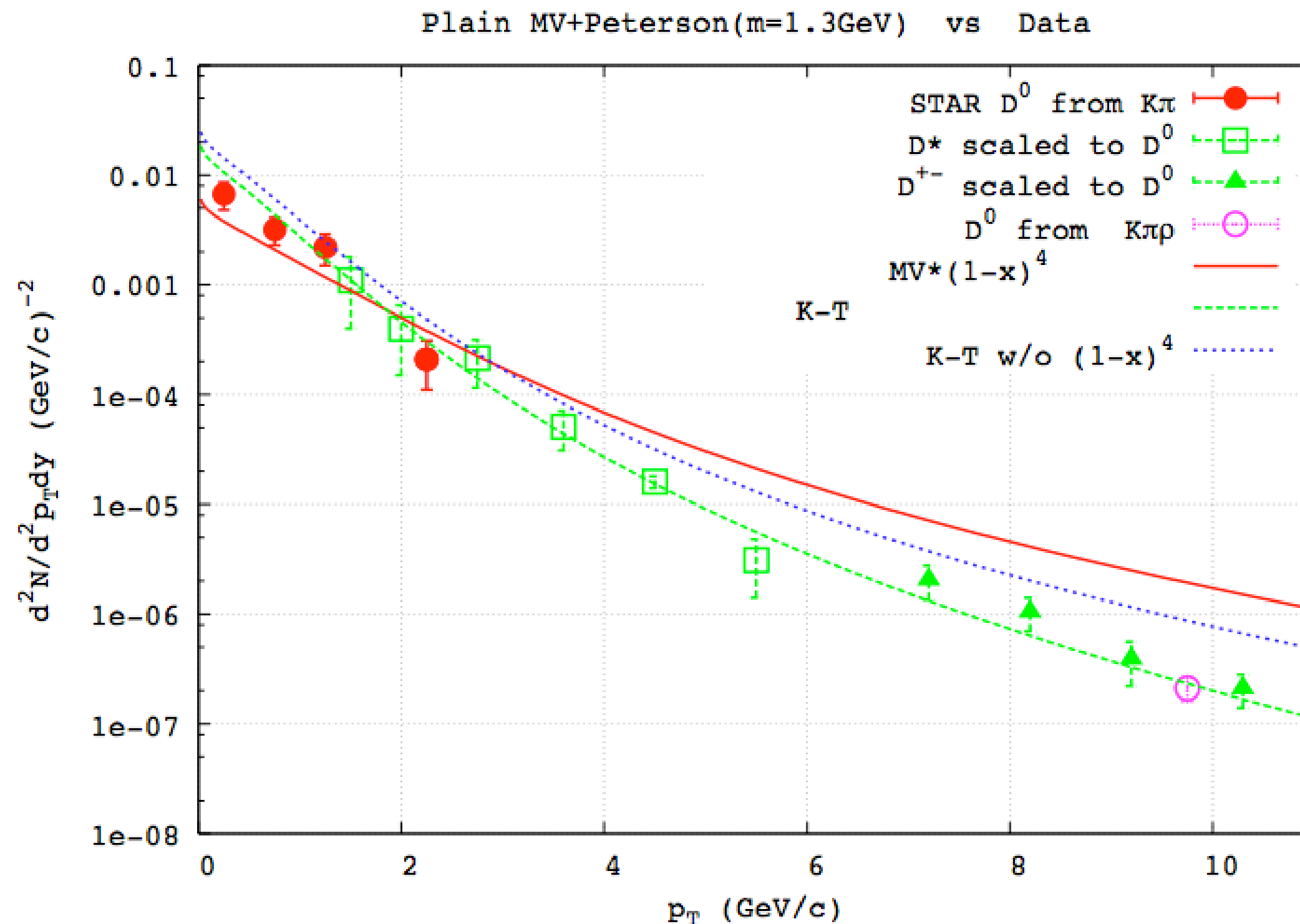


# Data from PHENIX



- Both suppression at forward rapidity and enhancement at backward one are consistent with CGC.

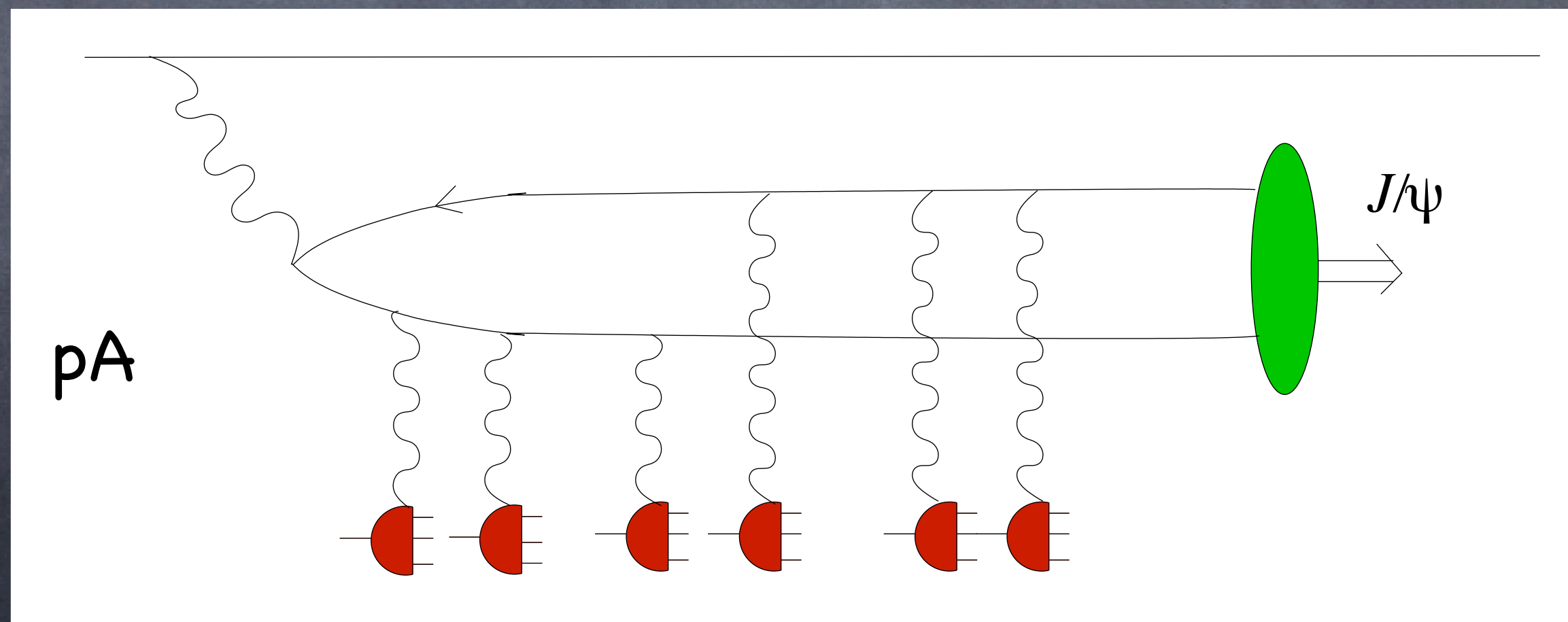
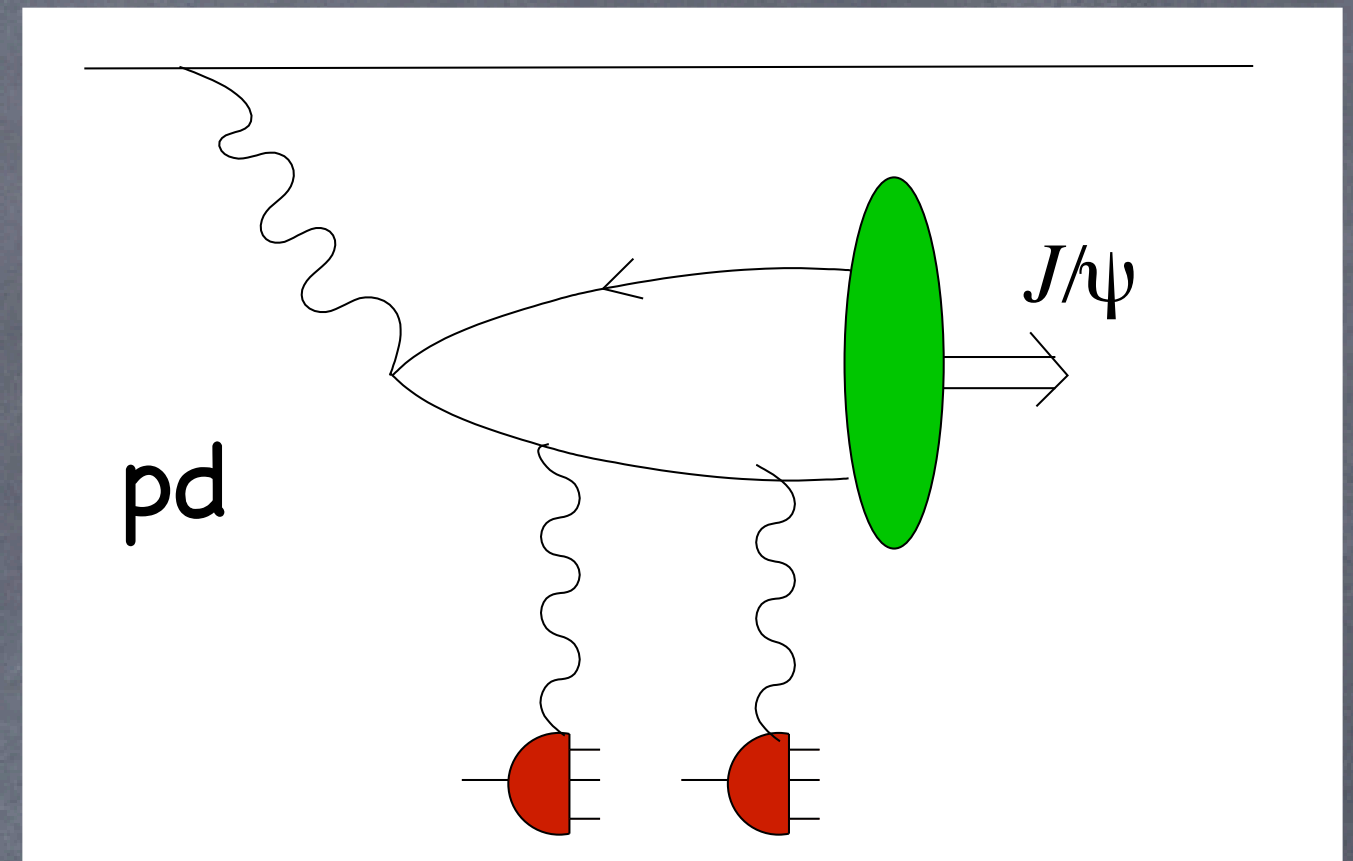
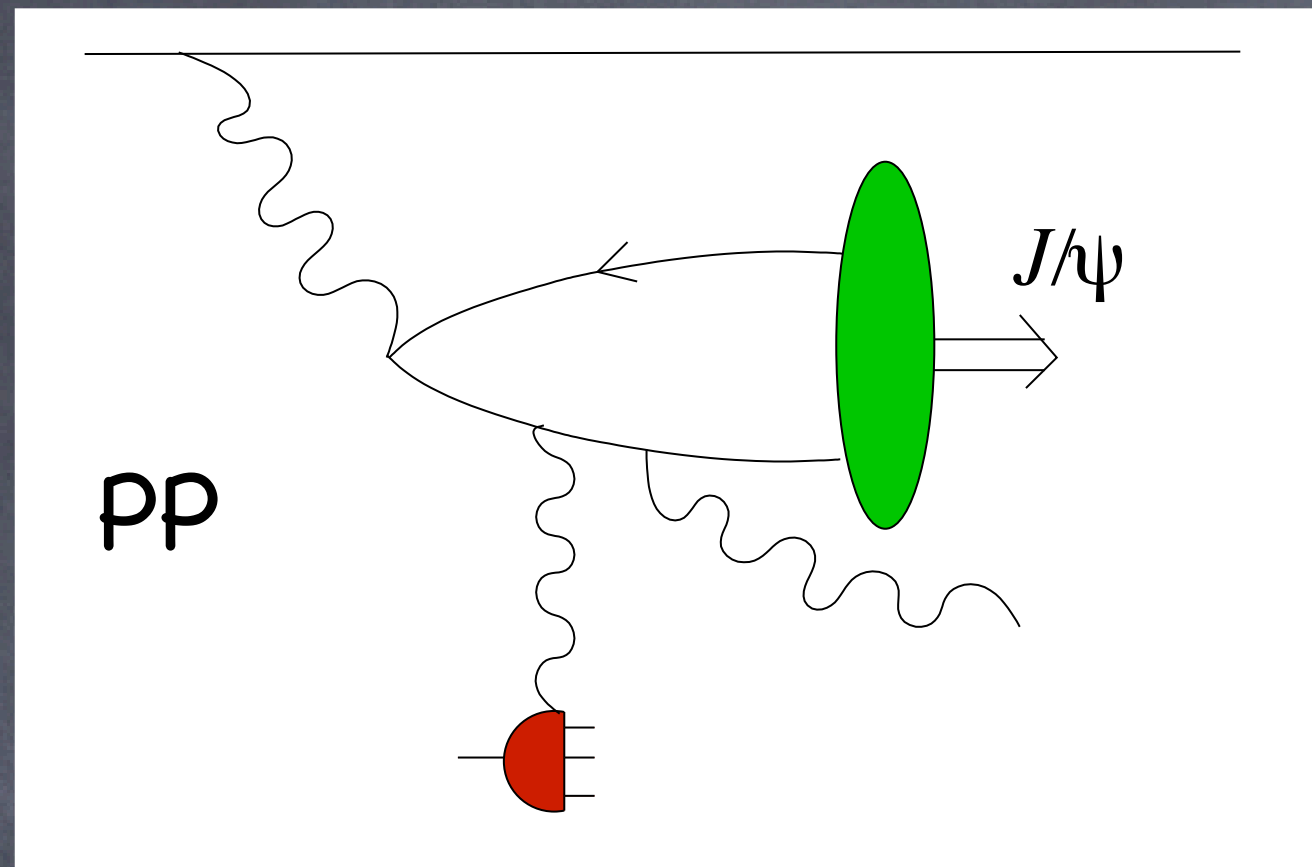
# Heavy Quark Spectrum



courtesy by R. Venugopalan

# $J/\psi$ production

Kharzeev and KT

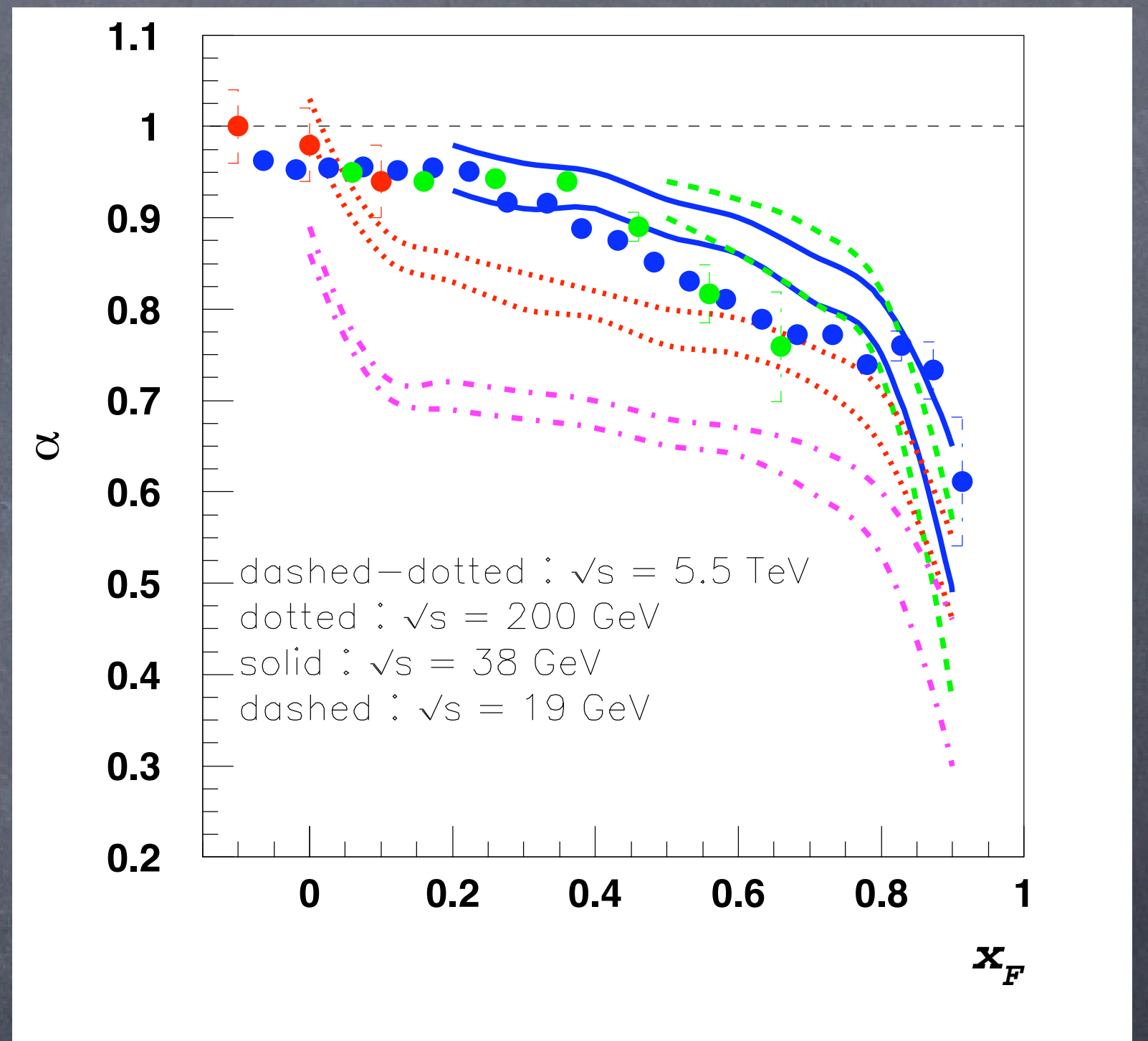
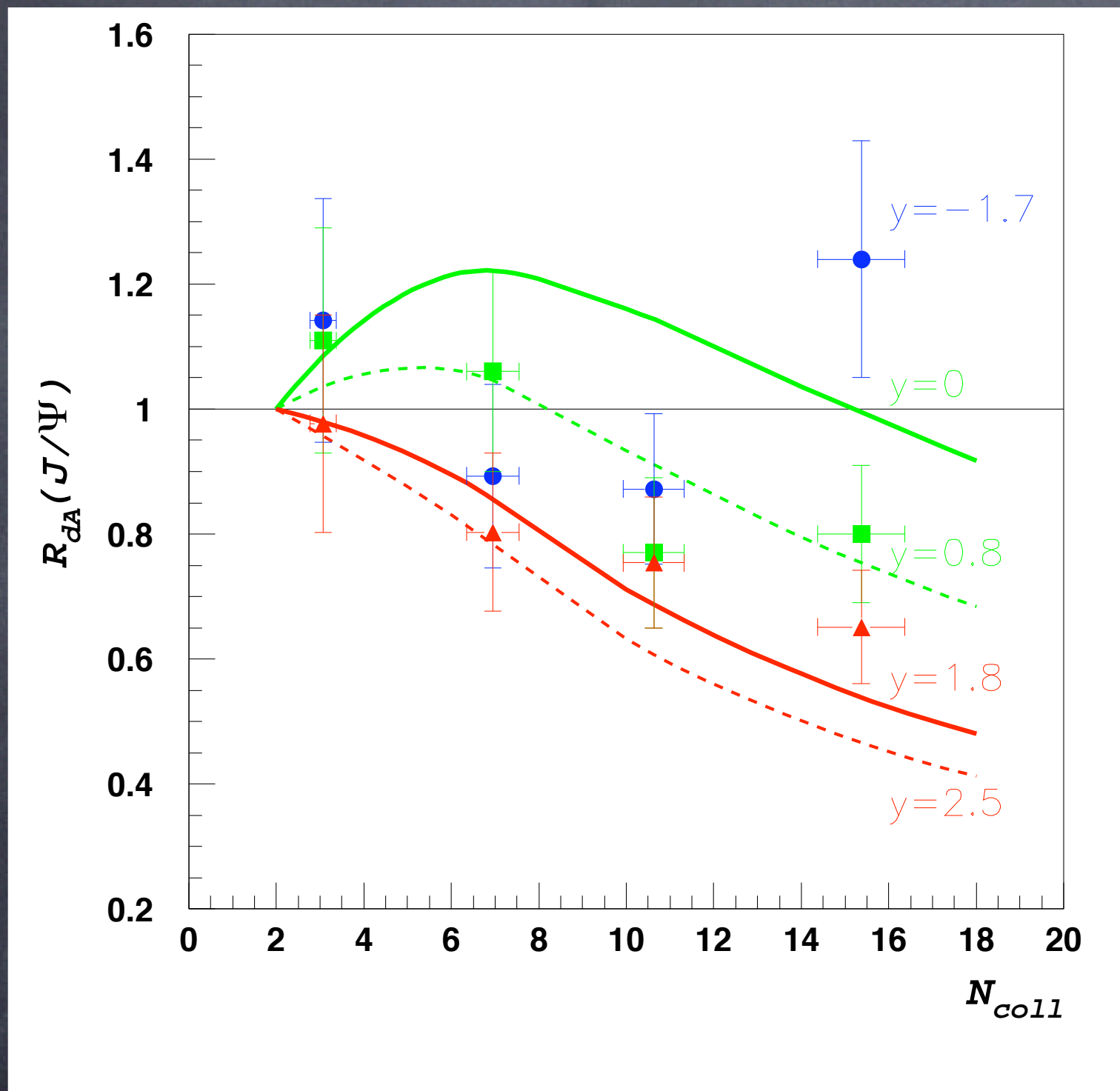




# $J/\psi$ production

Kharzeev and KT

" $x_F$ -scaling"

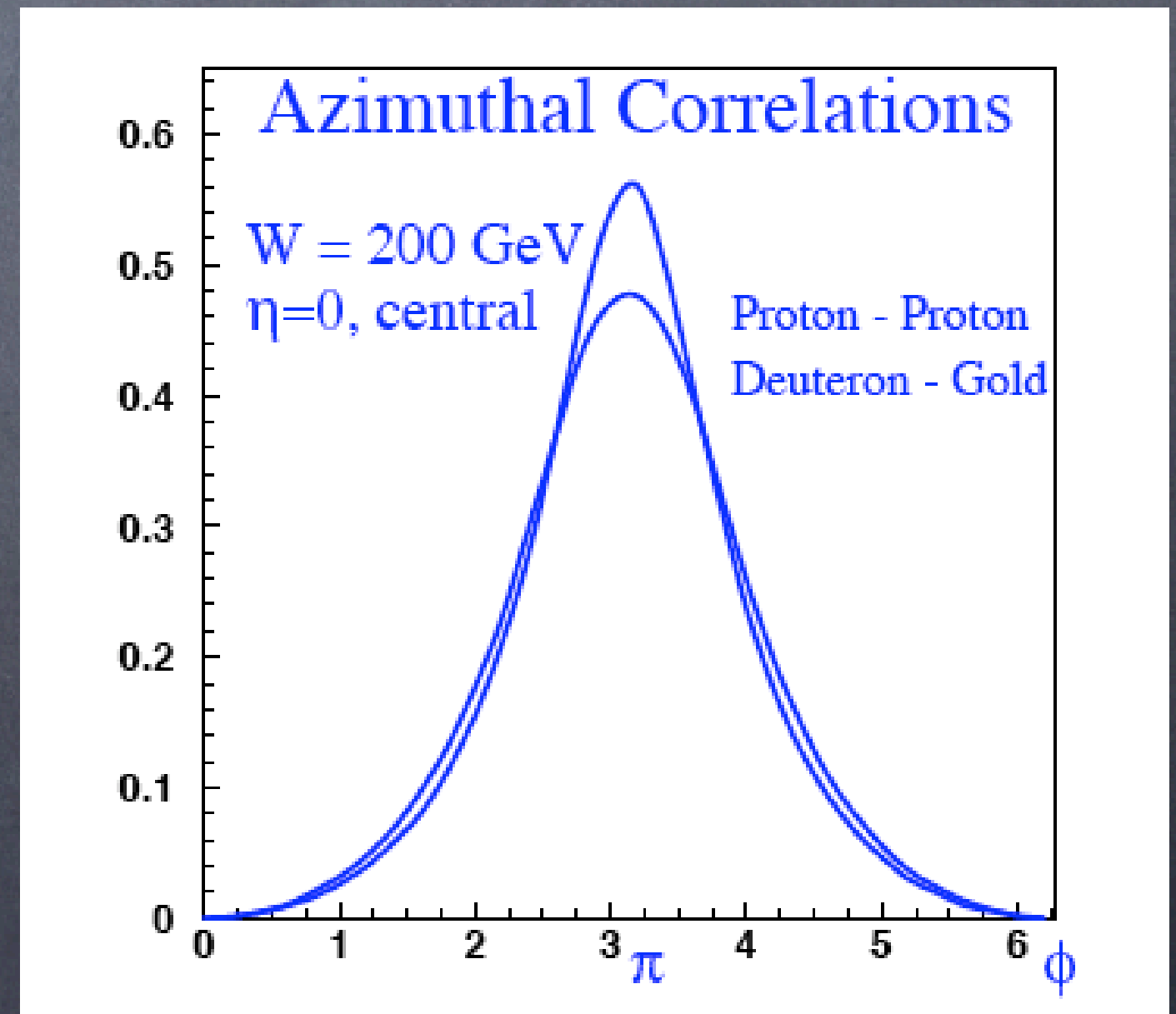
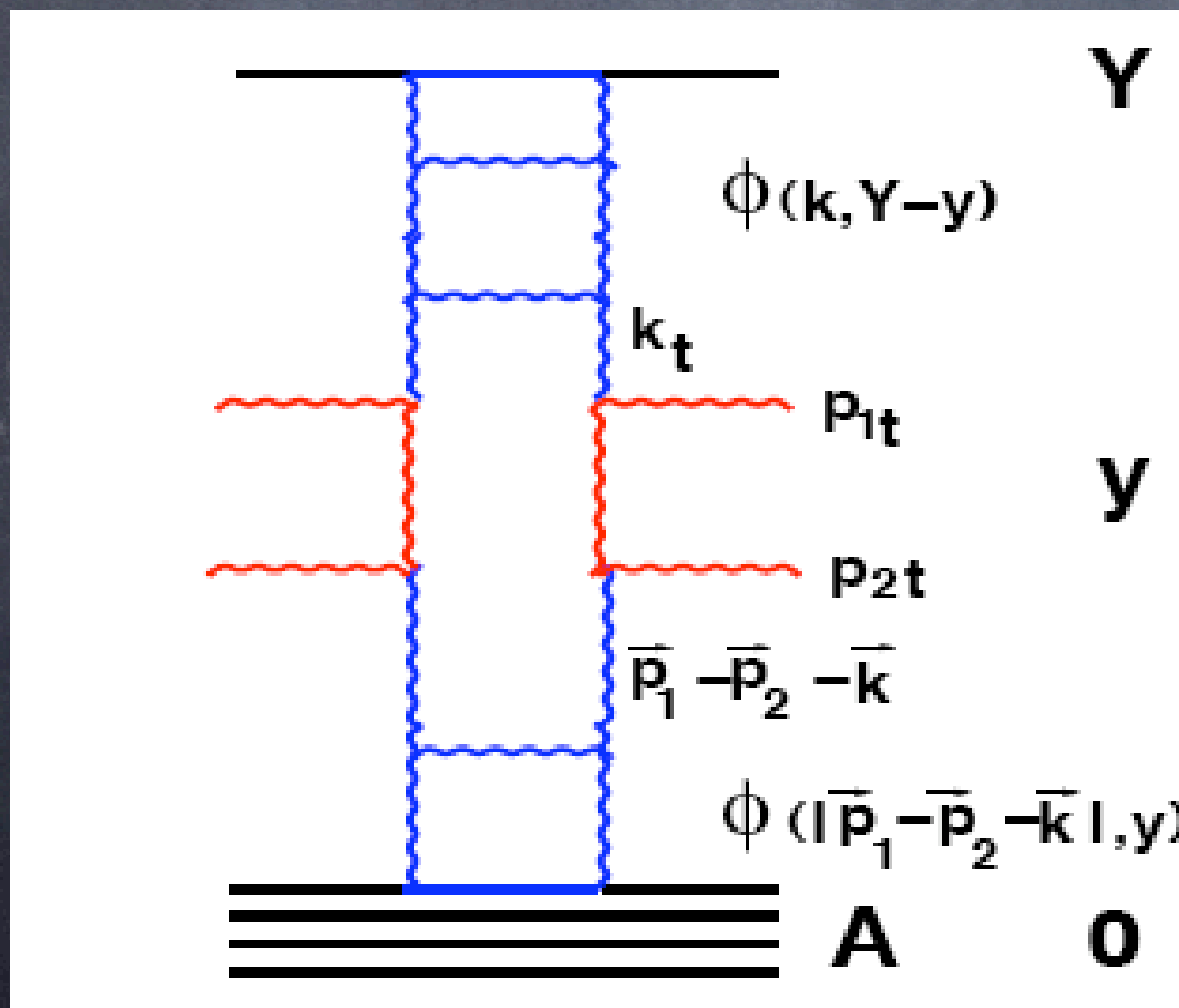


data by PHENIX

more details  
in the talk by  
Alex Kovner

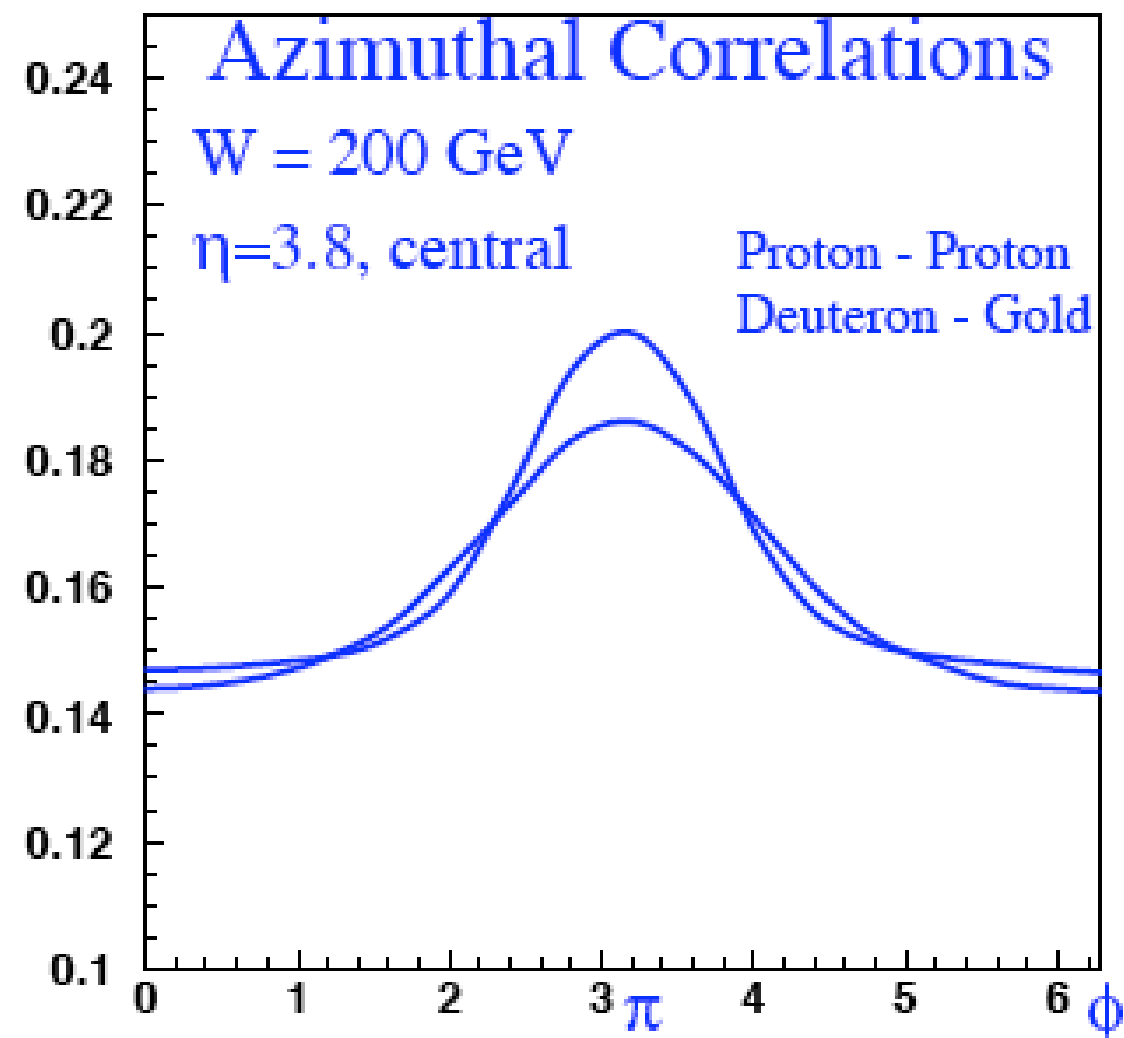
## Azimuthal correlations

- Azimuthal correlations due to CGC are different from pQCD: they are depleted since the classical fields commute. Prediction (Kharzeev, Levin, McLerran): suppression of back-to-back correlation at low  $x$ .

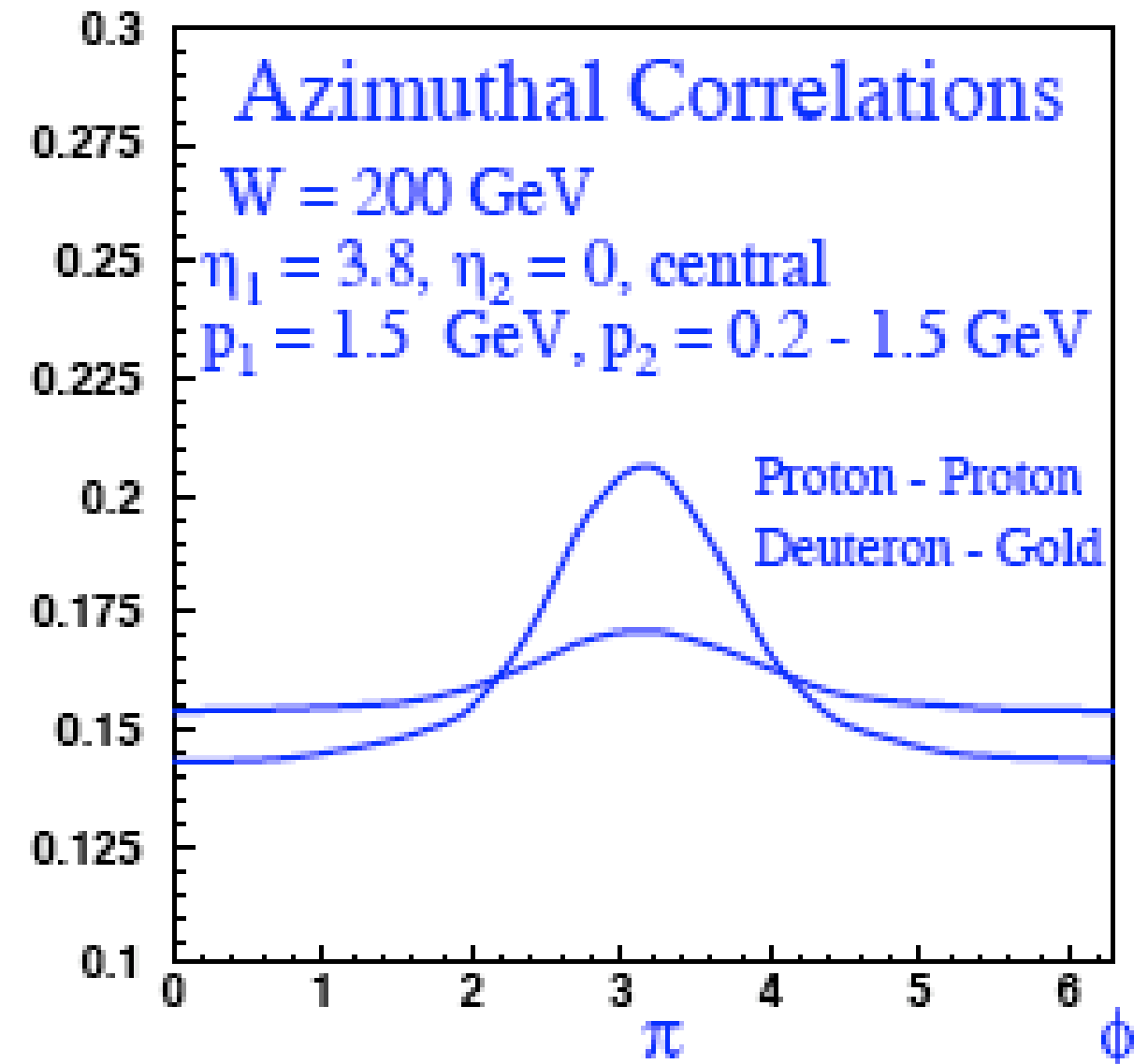


# Azimuthal correlations

- at forward rapidity:



- backward-forward correlations:

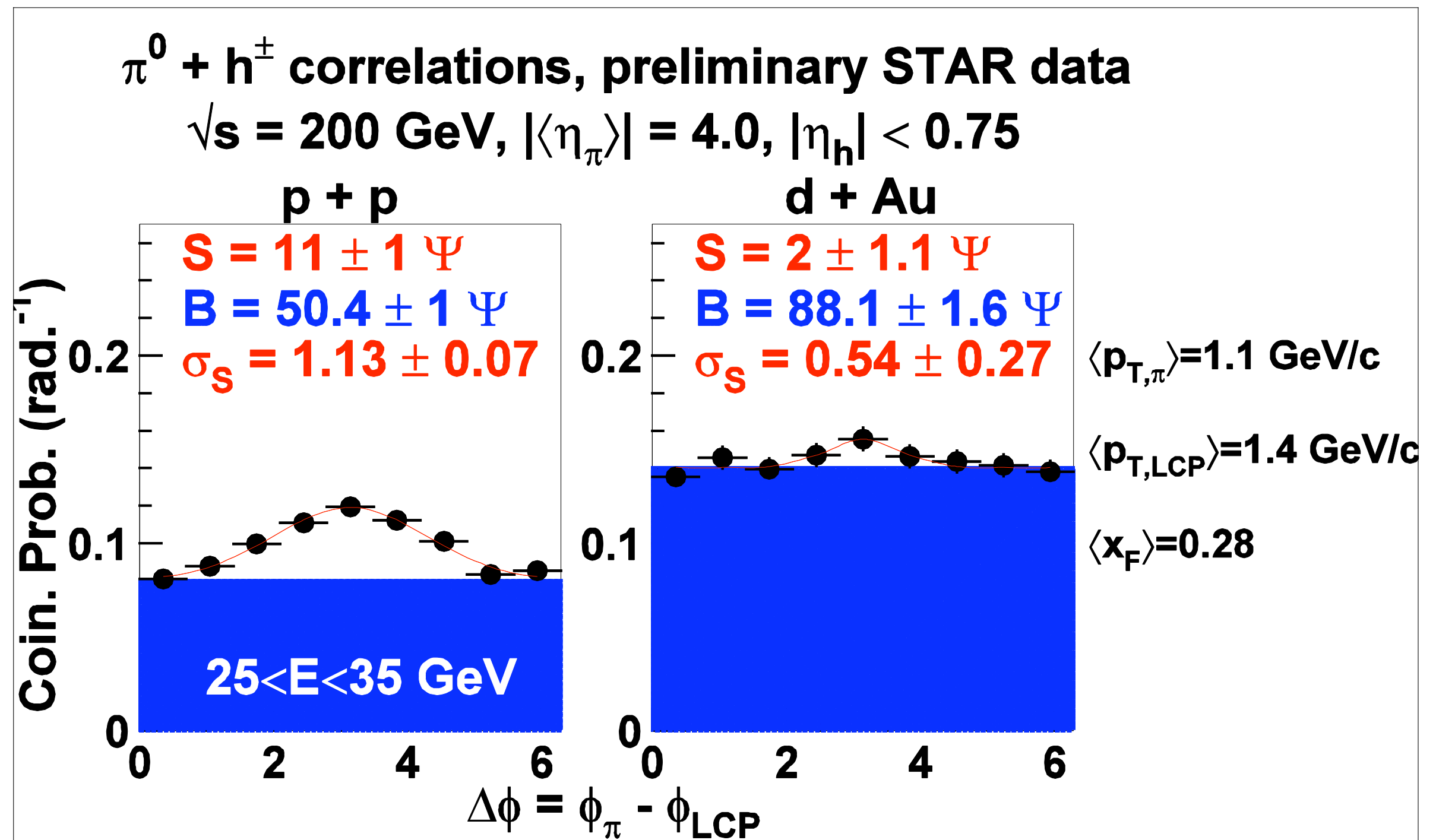


- Exact calculation of the double inclusive gluon production see Jalilian-Marian, Kovchegov.

see also Baier, Kovner, Nardi, Wiedemann

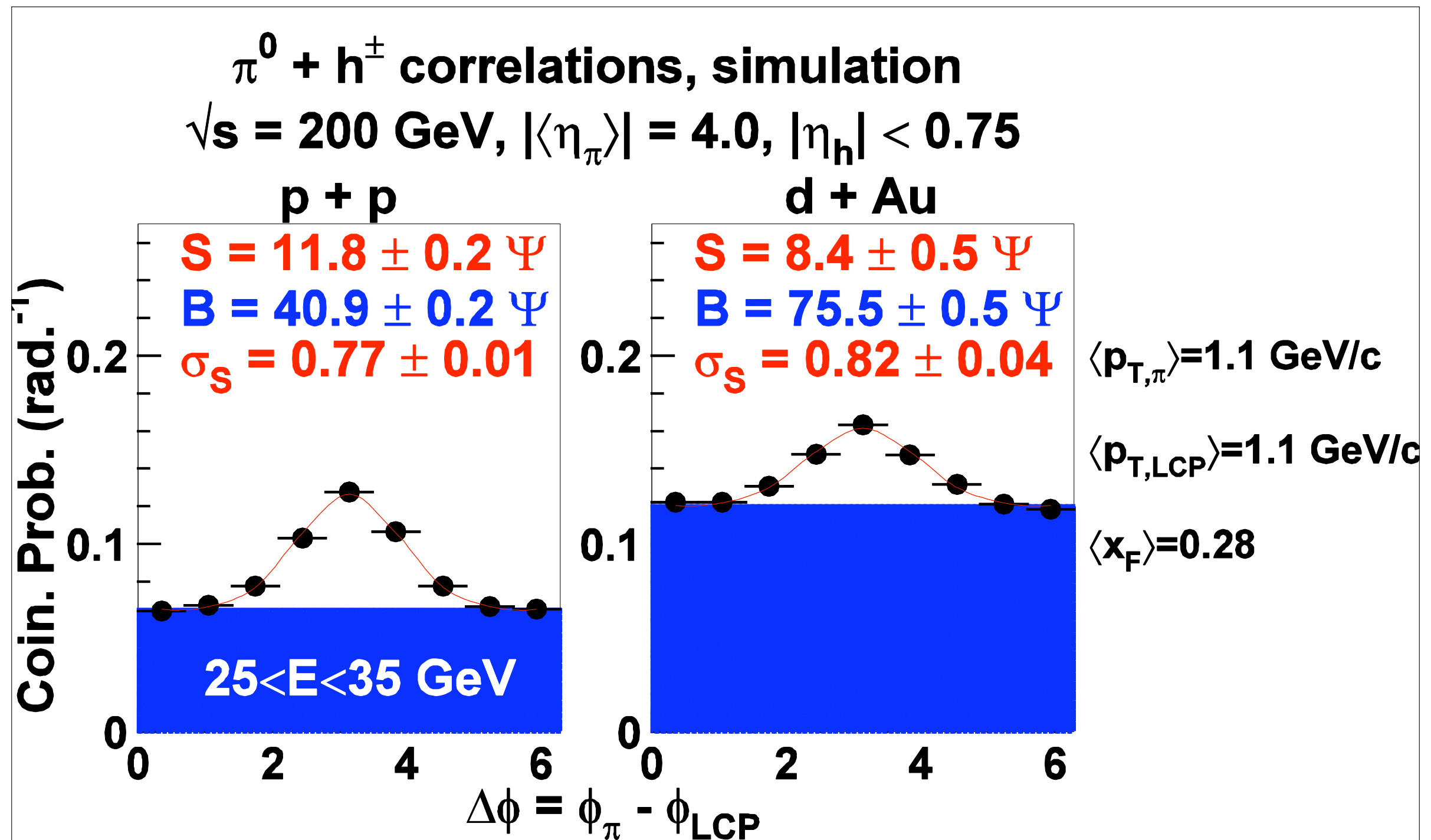


# Back-to-back correlations



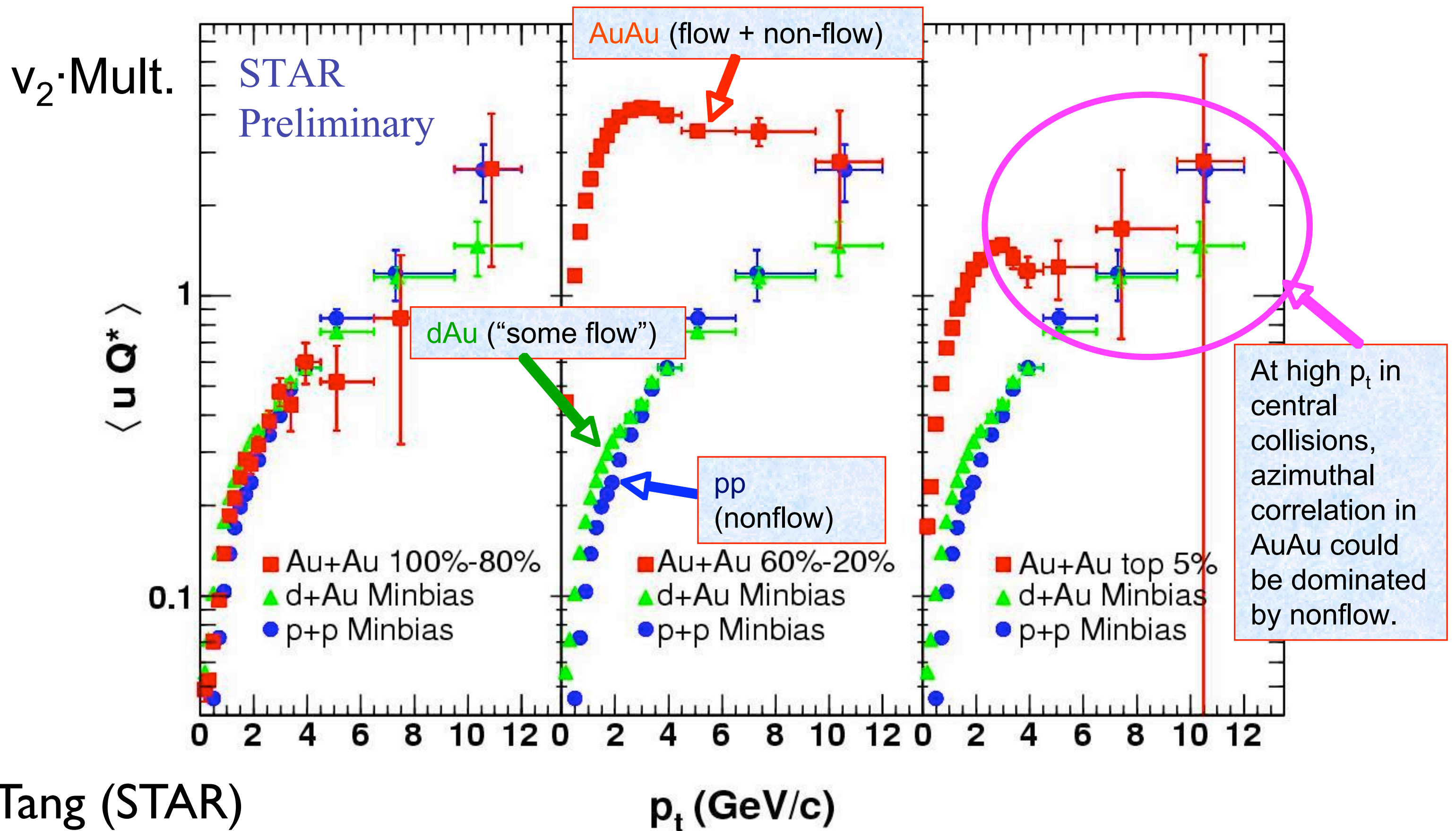
by STAR

# Back-to-back correlations



from HIJING

# Azimuthal correlations in AuAu, dAu and pp



by Tang (STAR)

There is a significant “flow” component in dA and pp at large  $p_T$   
(Kovchegov, KT)

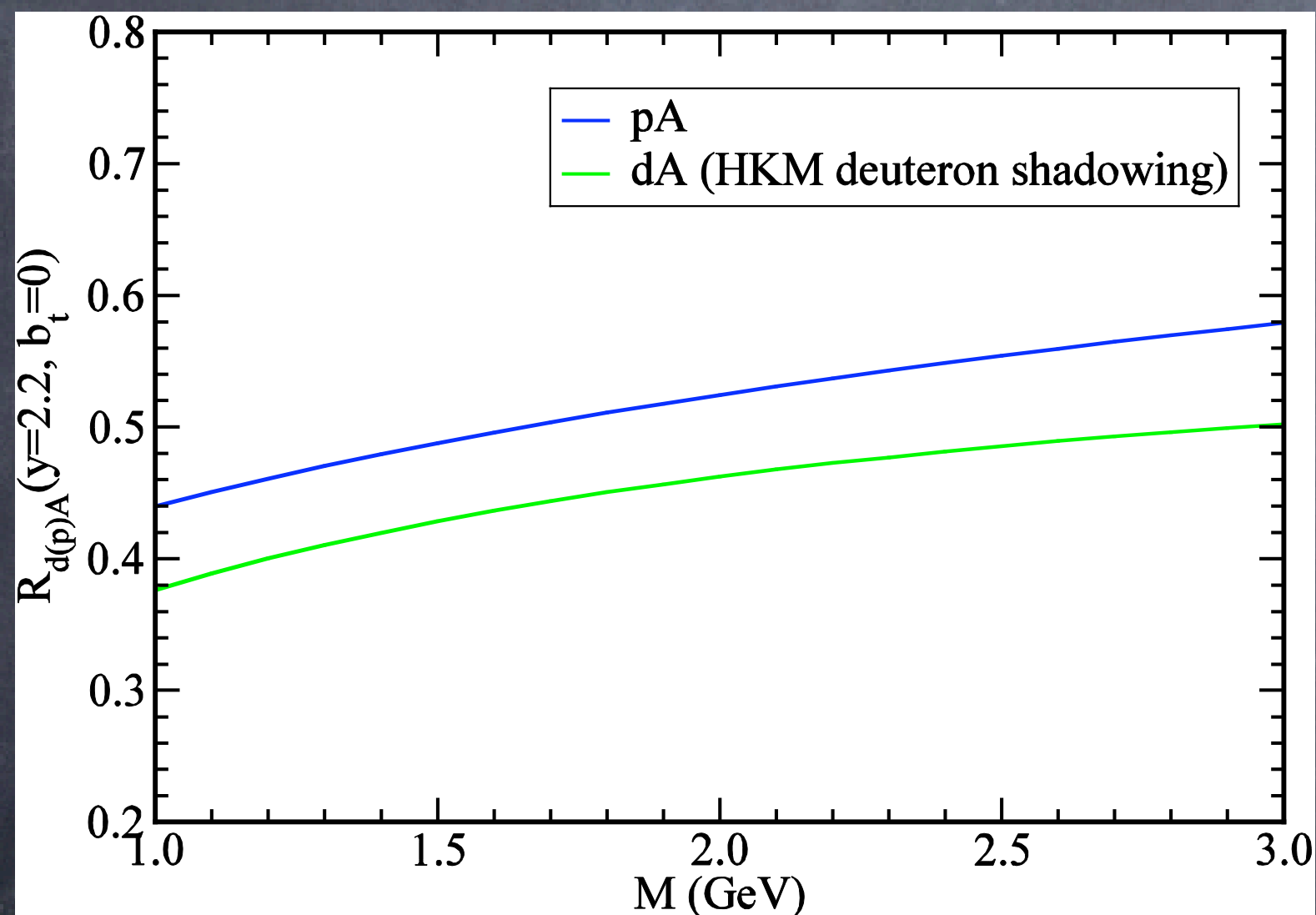


# Di-lepton production

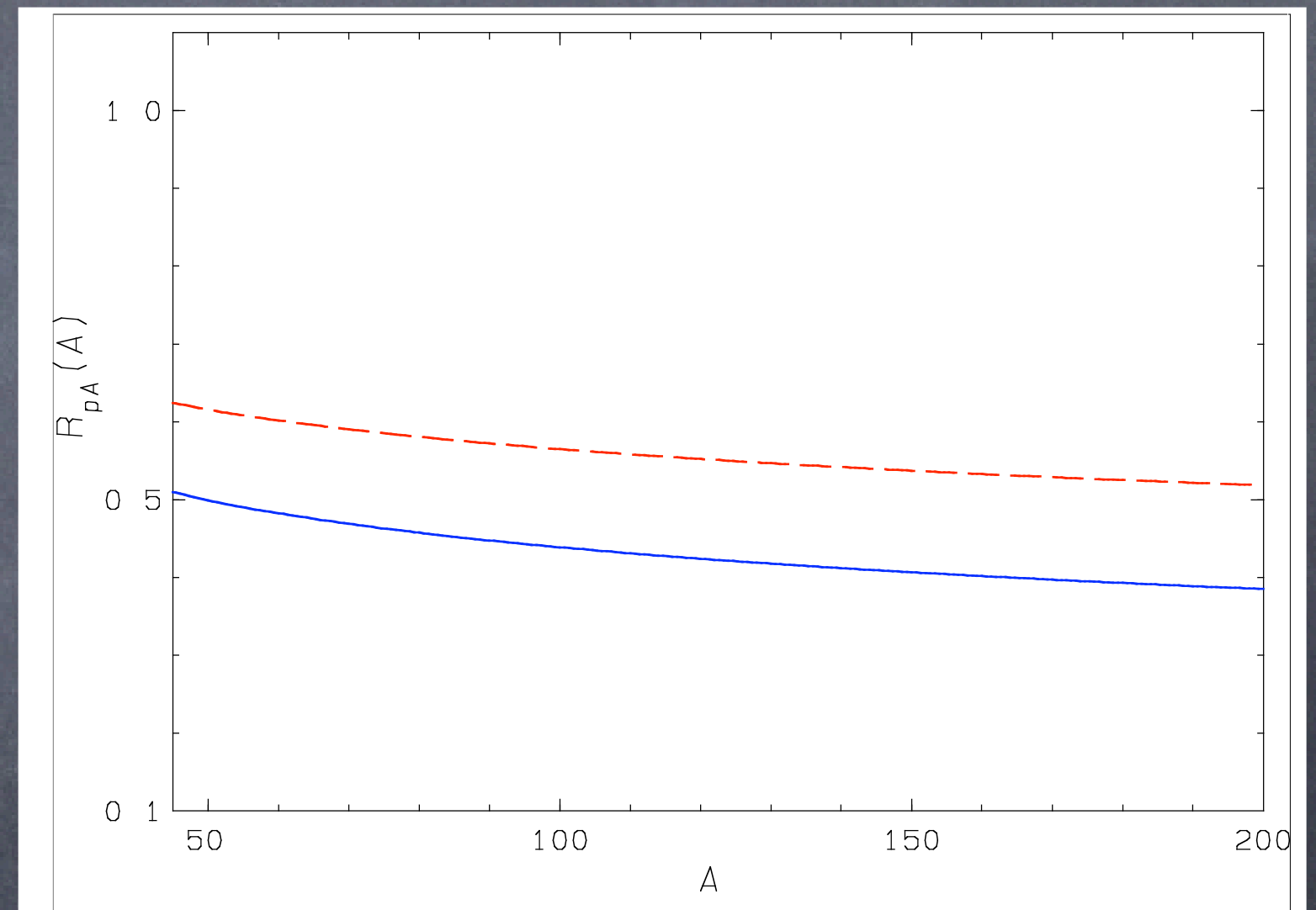
## Advantages of di-leptons:

- ✓ no need to know the fragmentation functions;
- ✓ do not strongly interact.

Kopeliovich, Schafer,  
Tarasov, (photons\*);  
Jalilian-Marian;  
Baier, Mueller, Schiff



$R_{dA}(M)$  integrated over transverse momenta of lepton pair (Jalilian-Marian)



$R_{dA}(A)$  at  $k_T=5$  GeV,  $M=2$  and  $y=3$   
(Baier, Mueller, Schiff)

# Summary: signatures of CGC in $p(d)A$

- Hadron spectra and multiplicities ✓
- Heavy quark spectra and multiplicities ✓ (preliminary)
- $J/\psi$   $\pm$
- Correlations  $\pm$
- Di-leptons ?
- Energy dependence - LHC.